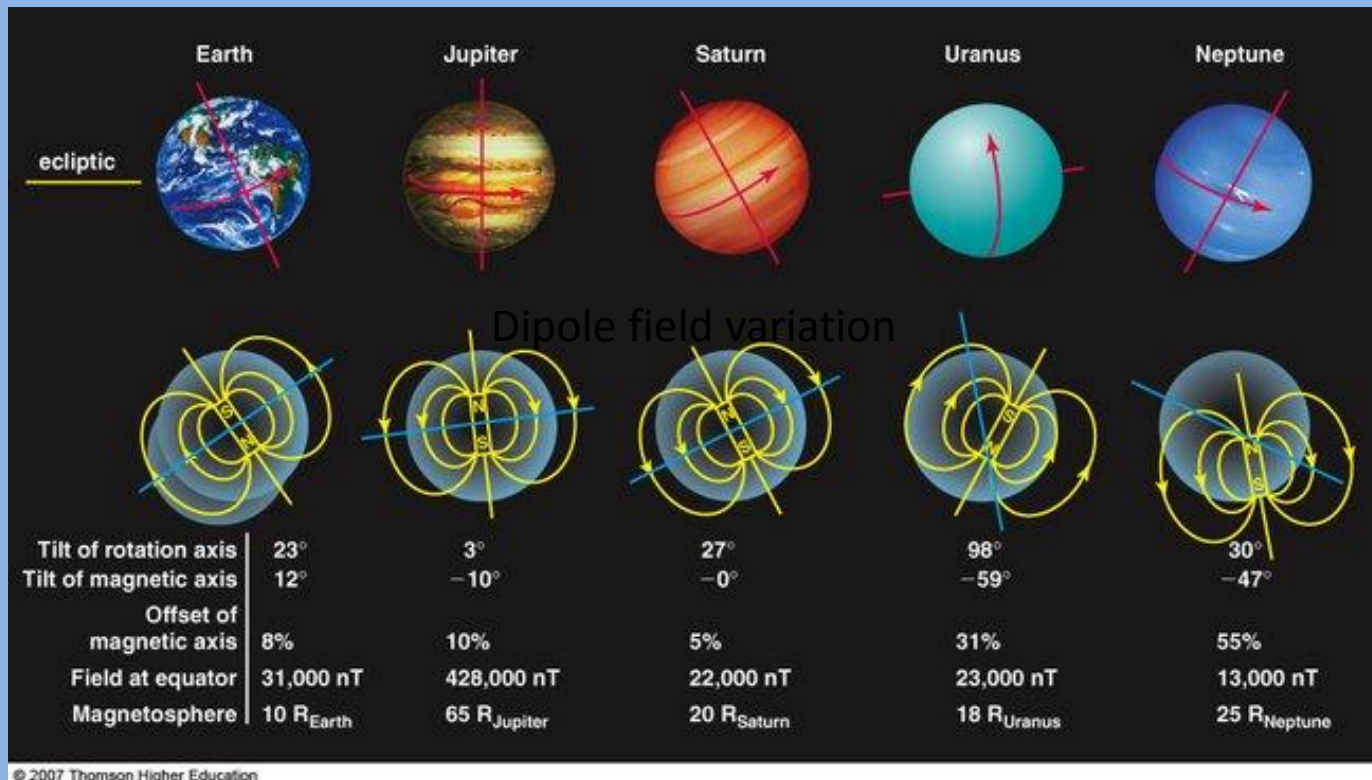


# Observational Constraints on Planetary Dynamos – What I think dynamo models should reflect!

Richard Holme  
University of Liverpool

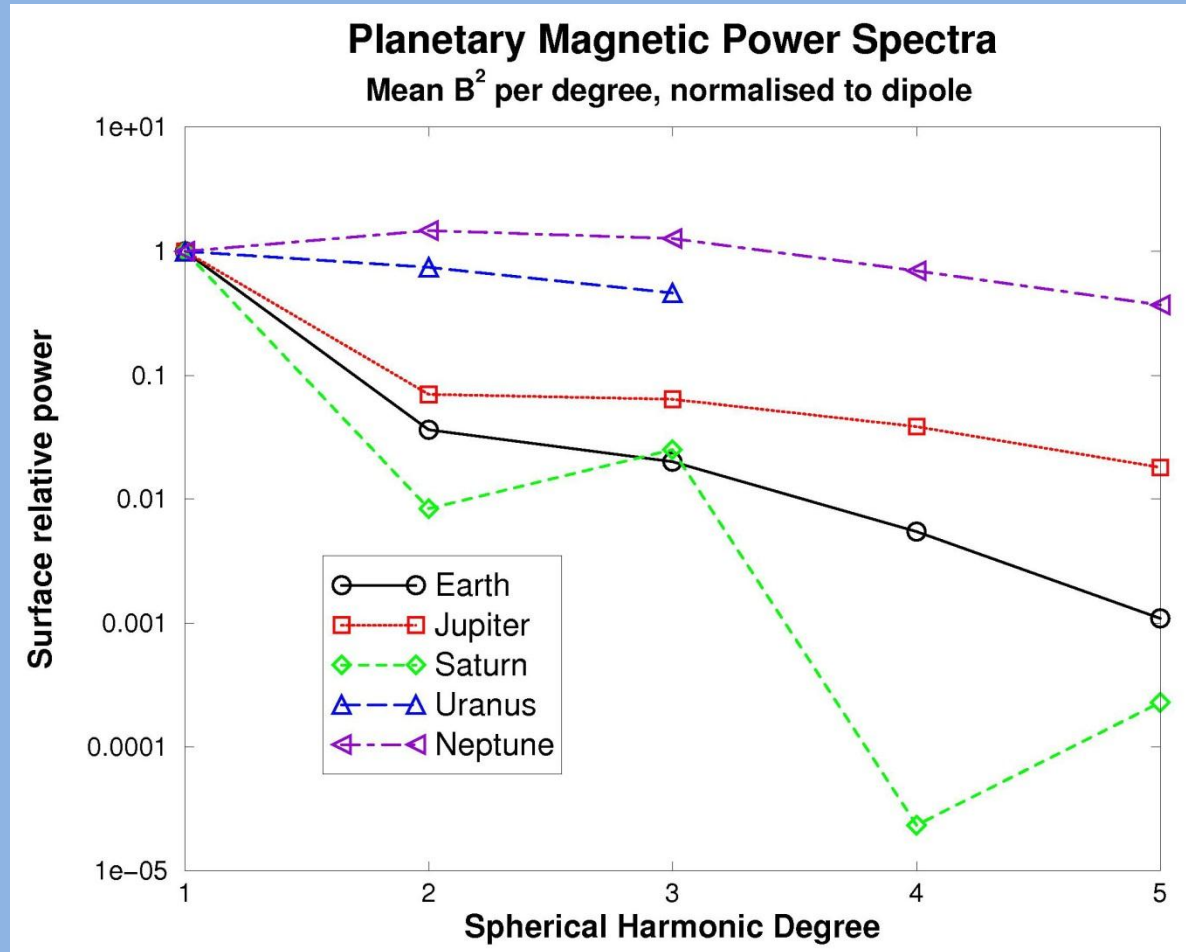
- Non-symmetry of fields of Uranus and Neptune
- Magnetic field and secular variation of Jupiter
- Geomagnetic secular variation spectrum
- Stable stratification and waves at the top of the Core
- Palaeointensity and inner core nucleation

# A Simple Picture



Fine for outreach and many external field studies  
Not fine for internal studies

# Power Spectra



Important constraint, but not everything

# Observational Constraints on Planetary Dynamos

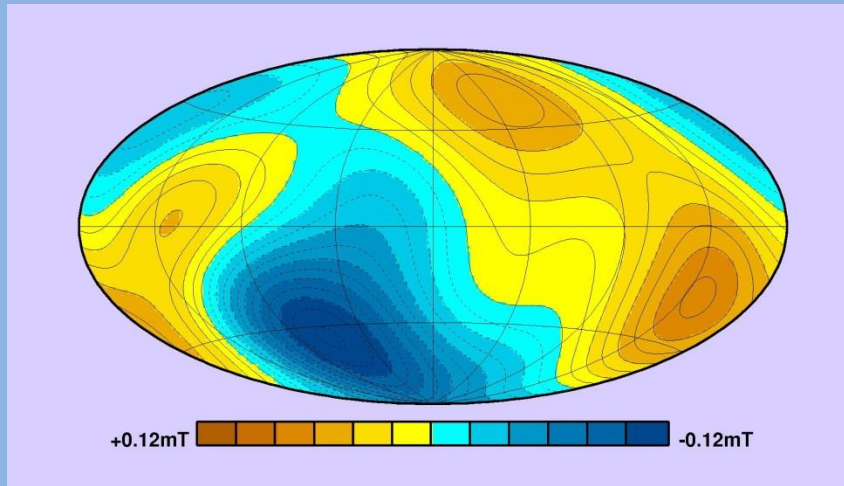
Richard Holme

University of Liverpool

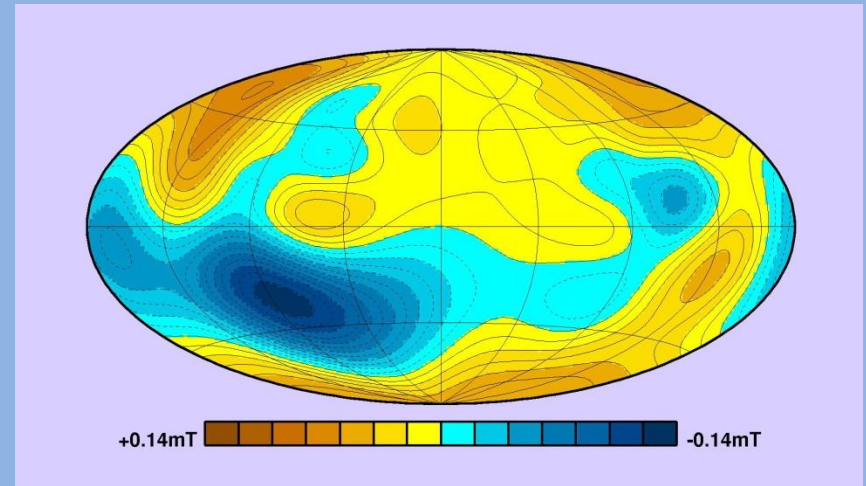
- **Non-symmetry of fields of Uranus and Neptune**
- Magnetic field and secular variation of Jupiter
- Geomagnetic secular variation spectrum
- Stable stratification and waves at the top of the Core
- Palaeointensity and inner core nucleation

# Uranus and Neptune Surface Fields

Uranus



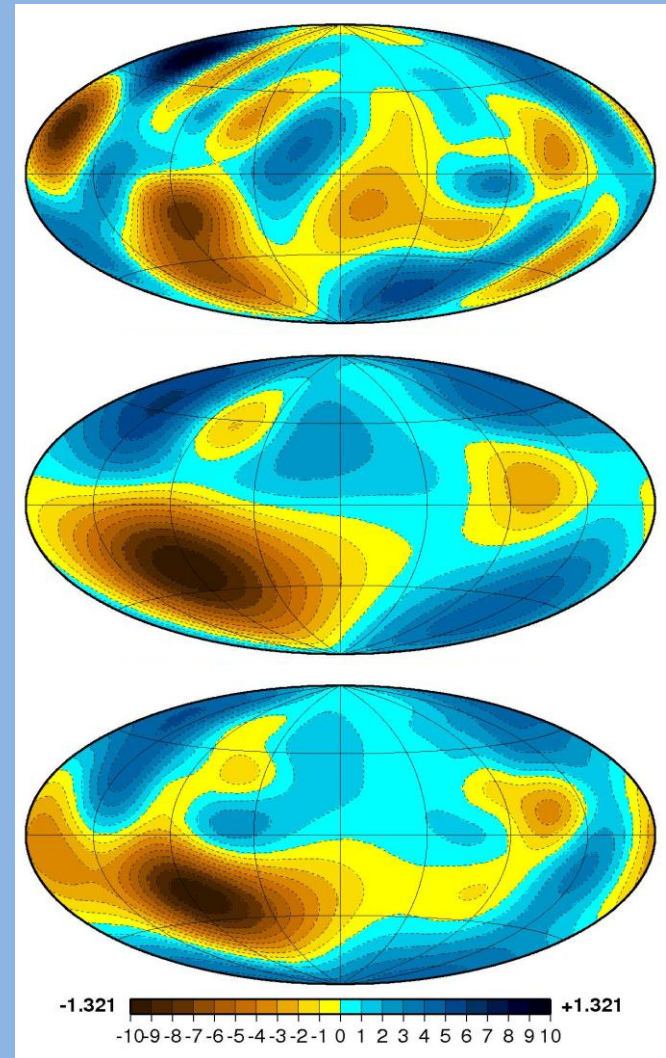
Neptune



- Very un-Earth-like – not dipolar even at surface
- Very different kind of field structure – differences in
  - Electrical conductivity?
  - Dynamical regime?
  - Energetics?

# Neptune field model range

- Three different models of surface field of Neptune
- All three models fit the data
- Decision for the modeller:
  - More complex model fits the data better, but is this detail required?
  - Simpler model fits well enough
  - Seek trade-off between explaining data and complexity



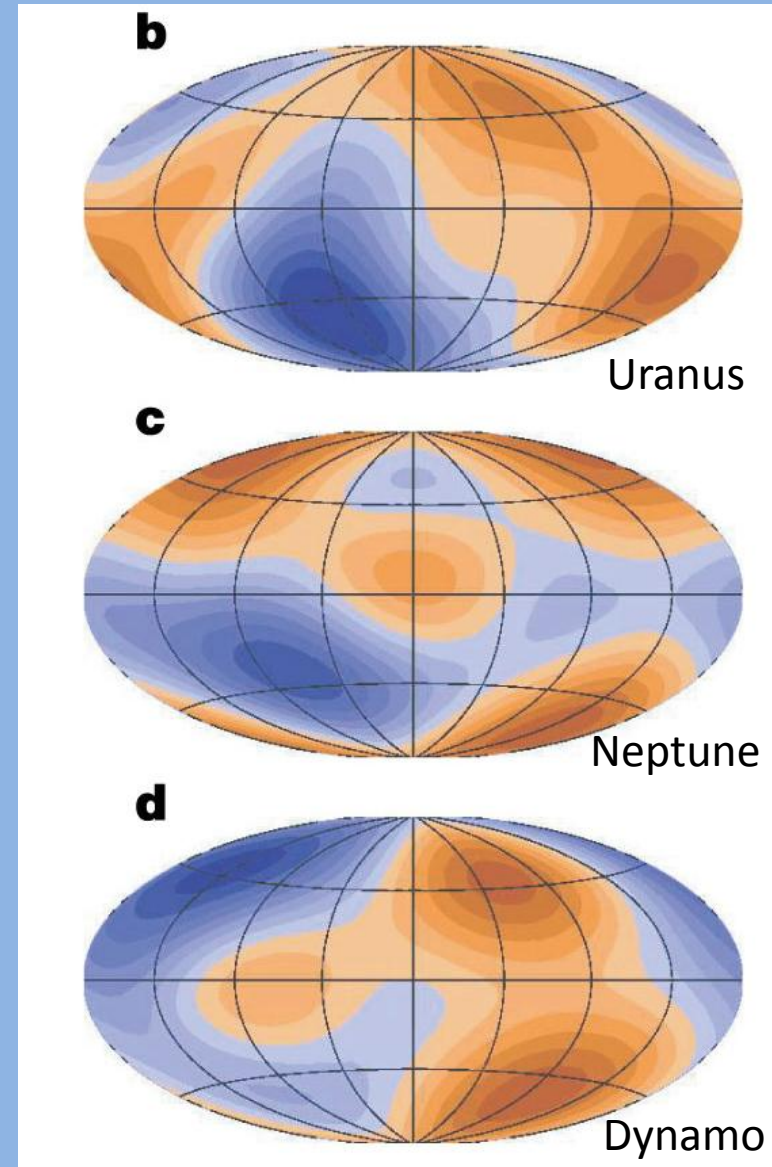


# Dynamo model interpretation

Comparison with observations  
not straightforward

- Example:
  - Truncate to common degree
  - Compare structure of field models from observations, dynamo
  - Similar complexity, power structure
- But – problem with too much symmetry
- Truncation losing information

**Solution – synthesise data from a dynamo model – invert and then compare**



# Observational Constraints on Planetary Dynamos

Richard Holme

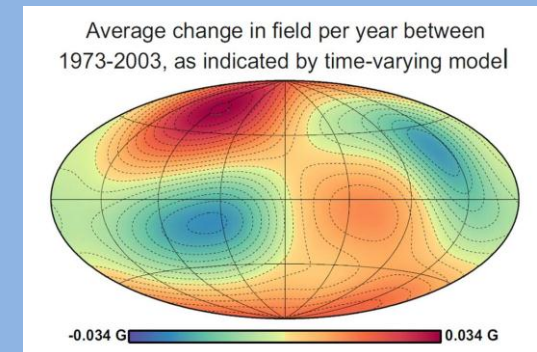
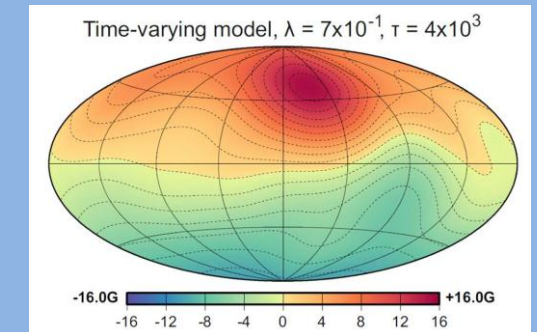
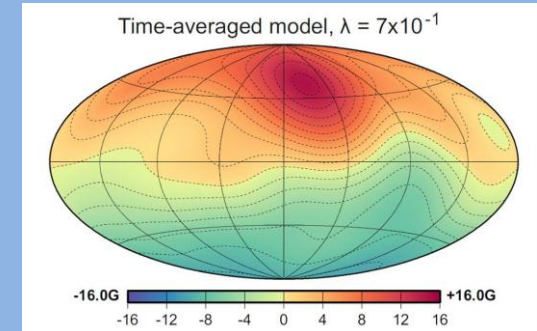
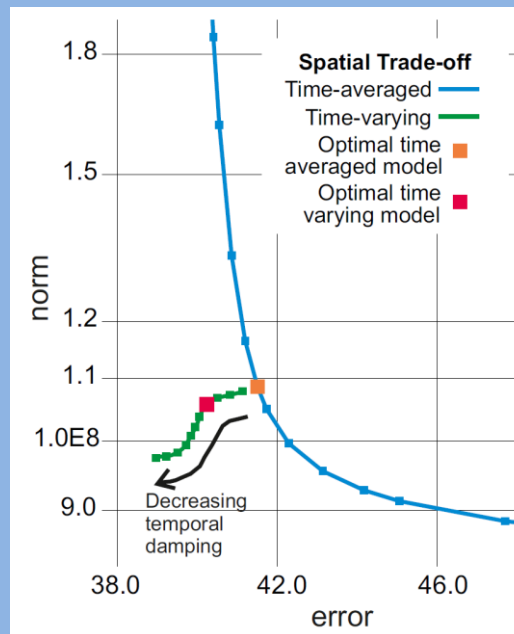
University of Liverpool

- Non-symmetry of fields of Uranus and Neptune
- **Magnetic field and secular variation of Jupiter**
- Geomagnetic secular variation spectrum
- Stable stratification and waves at the top of the Core
- Palaeointensity and inner core nucleation



# Models of Jovian Field Change

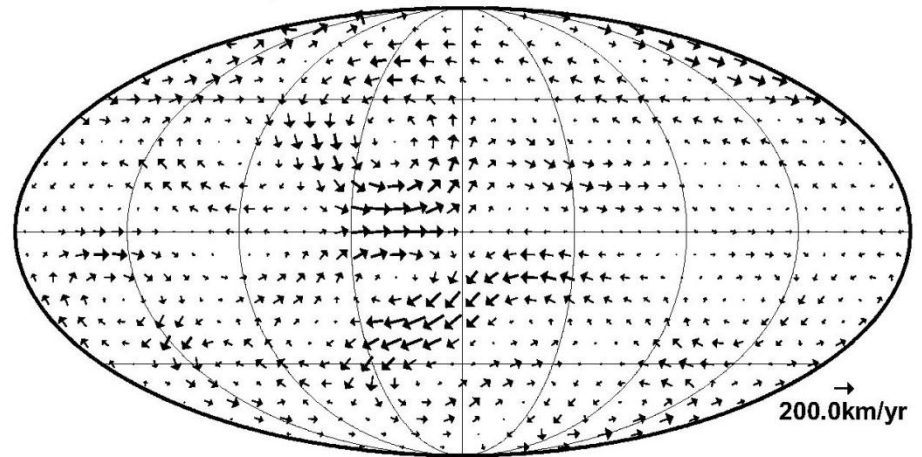
- Over 30 years of data from Pioneer to Galileo
- Dipole SV optimal model  $0.042\% \text{ yr}^{-1}$  (Earth  $\sim 0.06\% \text{ yr}^{-1}$ )
- Time variation not required – improvement in model better than increased spatial complexity (Models of Victoria Ridley)



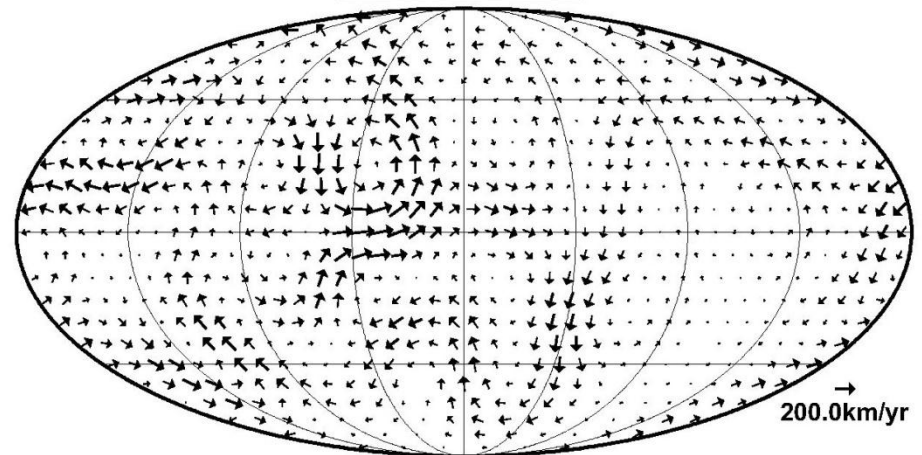
# Jovian Flow Modelling

- From SV models, can infer flow at top of core –  $0.85R_J$
- Require detailed flow structure to explain SV
- Cannot result from rotation alone

Tangentially geostrophic flow:

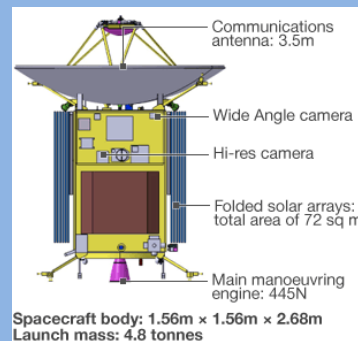
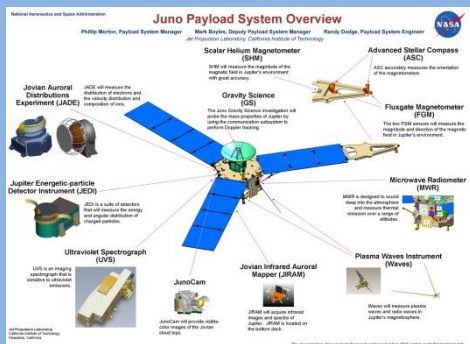
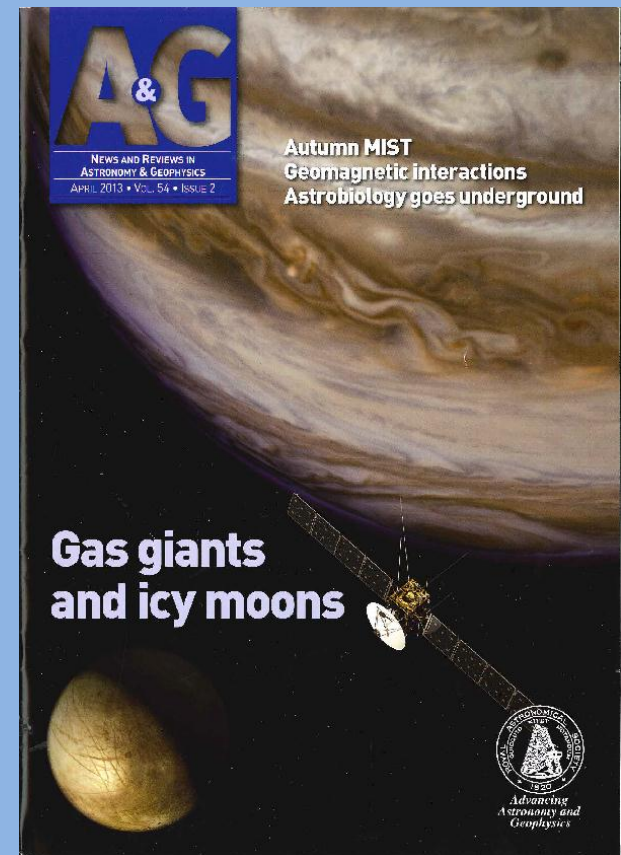
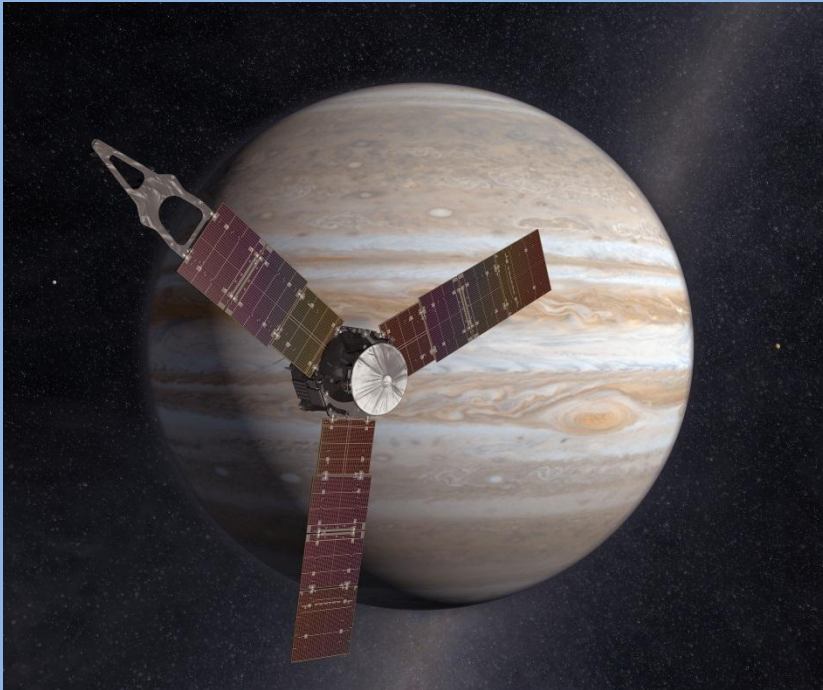


Toroidal flow:



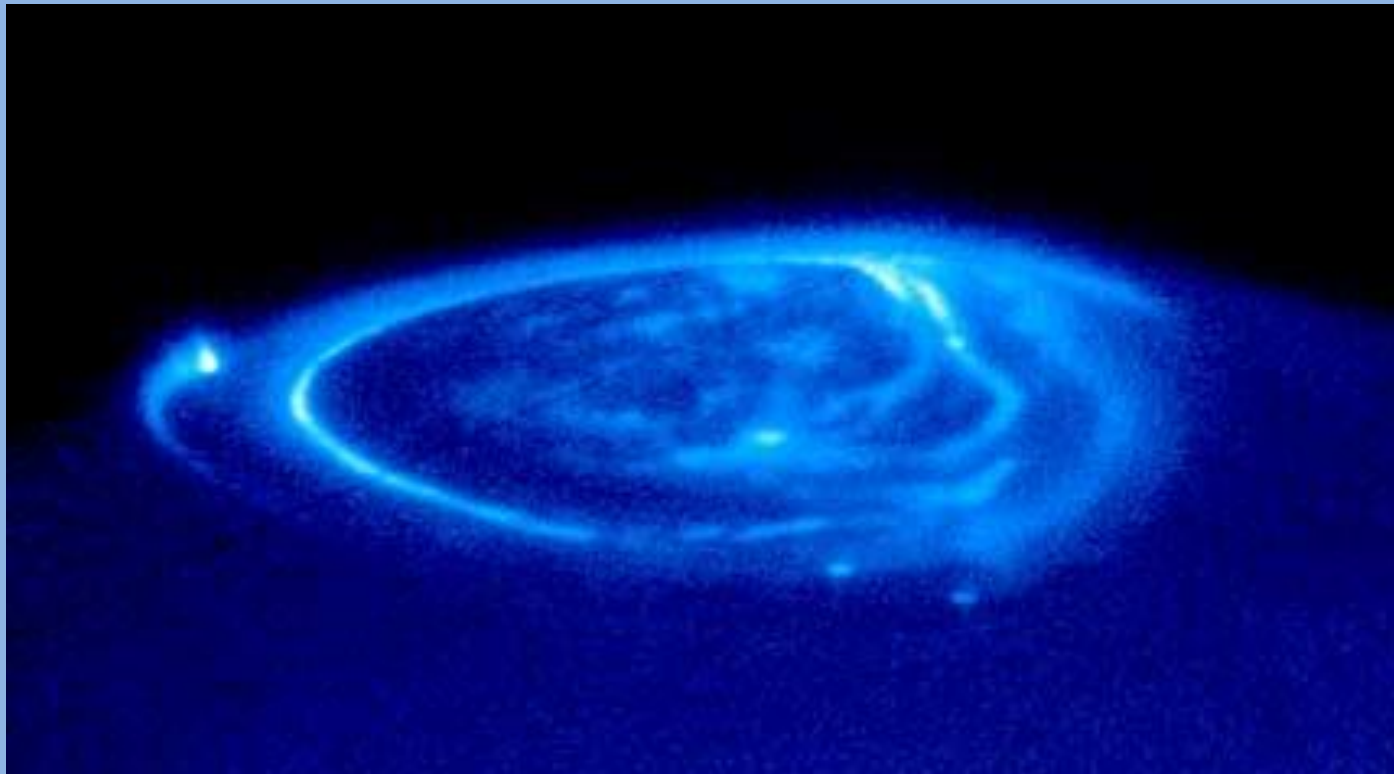
# New Jupiter Missions

## Juno and JUICE



# Magnetic field constraint from Aurora

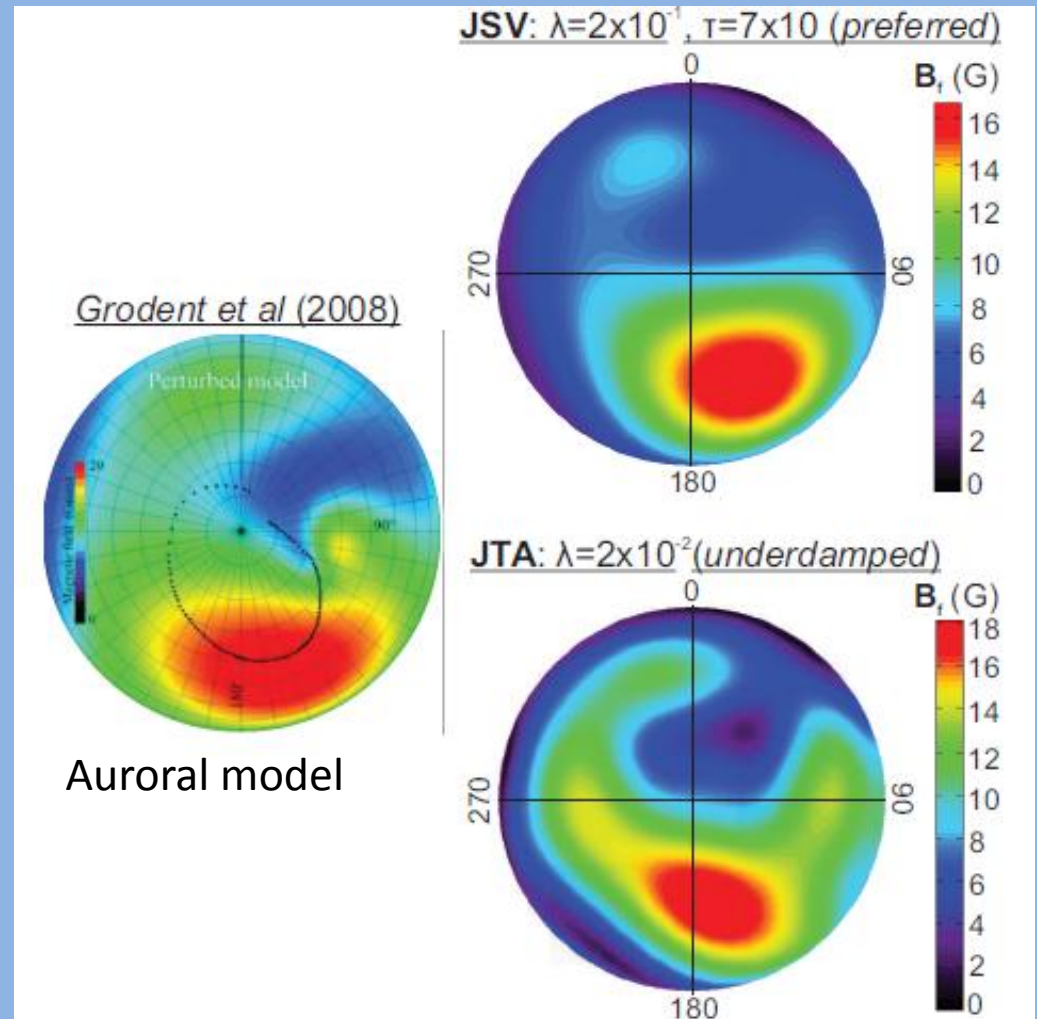
- Auroral structure and Galilean moon magnetic footprints provide high resolution field information
- Example from Hubble Space Telescope





# Is there more detail in the data?

- Models with auroral constraint higher resolution near the poles
- Compare models from satellite data alone
- Underdamped model not “fully converged” but features match higher-resolution auroral model
- More information in the data than we had thought?



# Observational Constraints on Planetary Dynamos

Richard Holme

University of Liverpool

- Non-symmetry of fields of Uranus and Neptune
- Magnetic field and secular variation of Jupiter
- **Geomagnetic secular variation spectrum**
- Stable stratification and waves at the top of the Core
- Palaeointensity and inner core nucleation

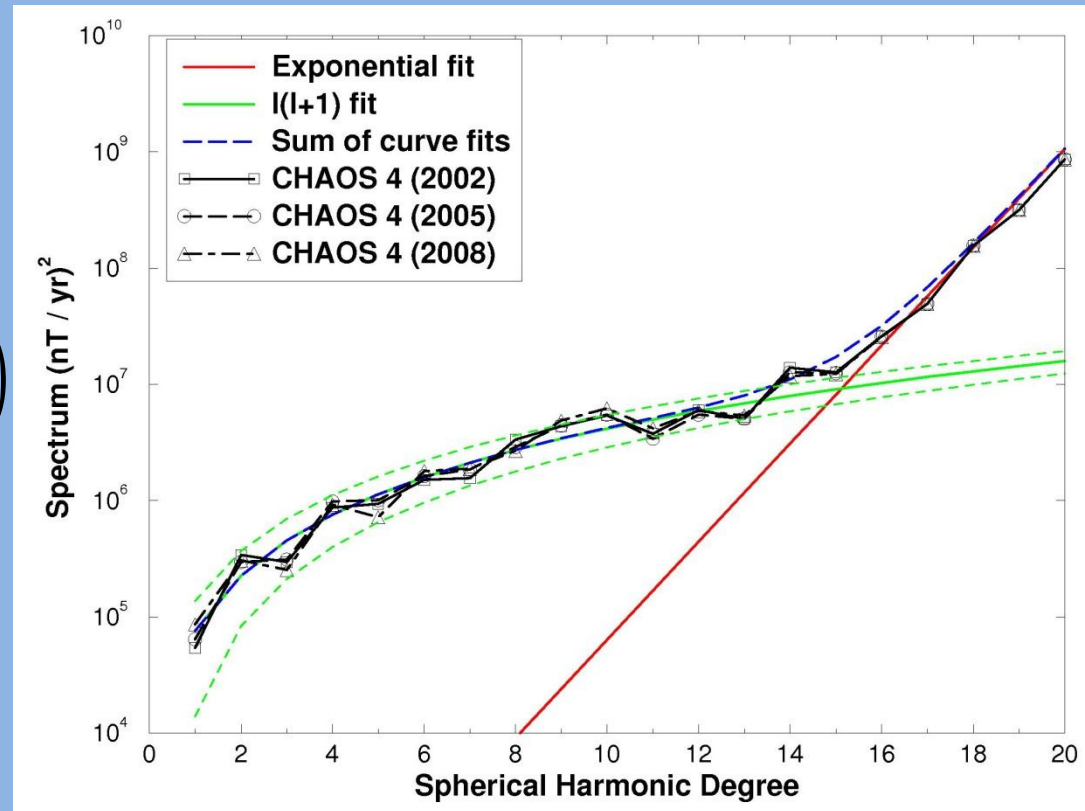


# Secular Variation Spectrum, CMB

- Secular variation - field time rate of change
- CMB spectrum:

$$\sum_{l=1}^{\infty} (l+1) \left( \frac{a}{c} \right)^{2l+4} \sum_{m=0}^l \left( (\dot{g}_l^m)^2 + (\dot{h}_l^m)^2 \right)$$

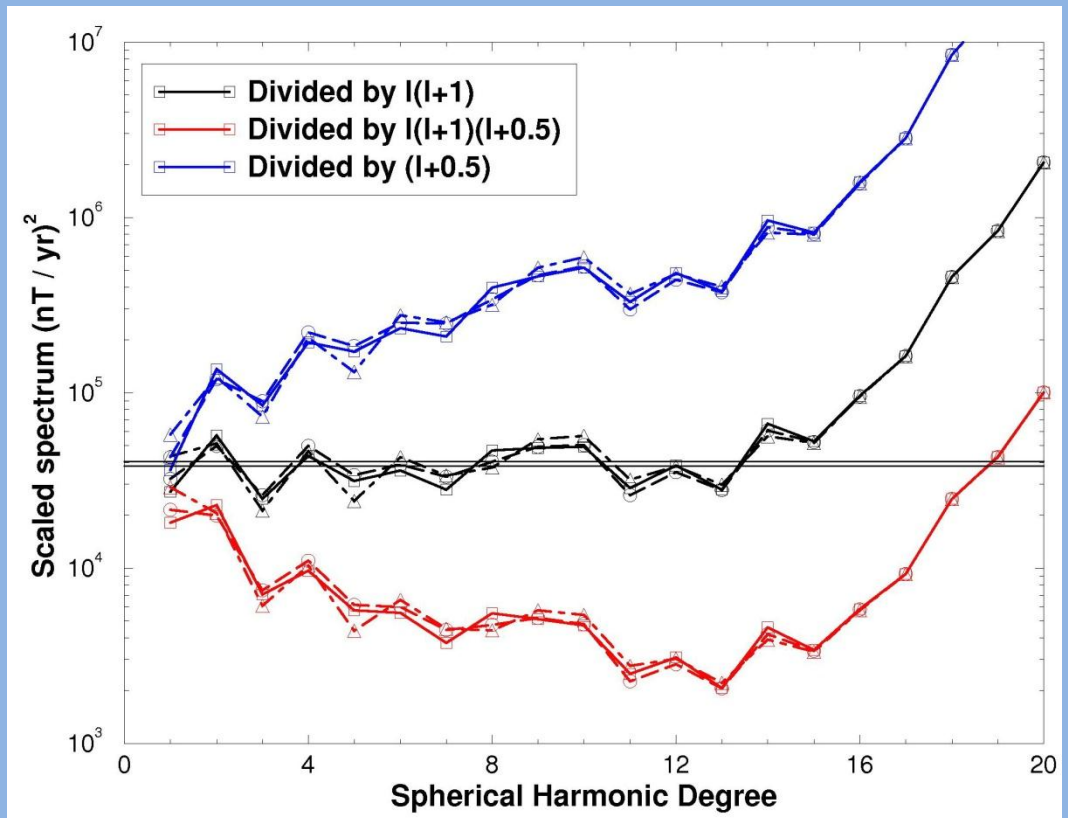
- Spectrum fit nicely by simple function of degree
- Fit so good tells us something about origin



# Other Possible Fits

- Single parameter fits proportional to
  - $l(l+1)(2l+1)$
  - $l(l+1)$  (or  $(2l+1)^2$ )
  - $(2l+1)$
- Theory to suggest top two (Voorhies)
- Third suggested from dynamo models
- All look good on log plots!
- $l(l+1)$  strongly preferred

Scaled Spectrum to test possible parameterisation



# Observational Constraints on Planetary Dynamos

Richard Holme

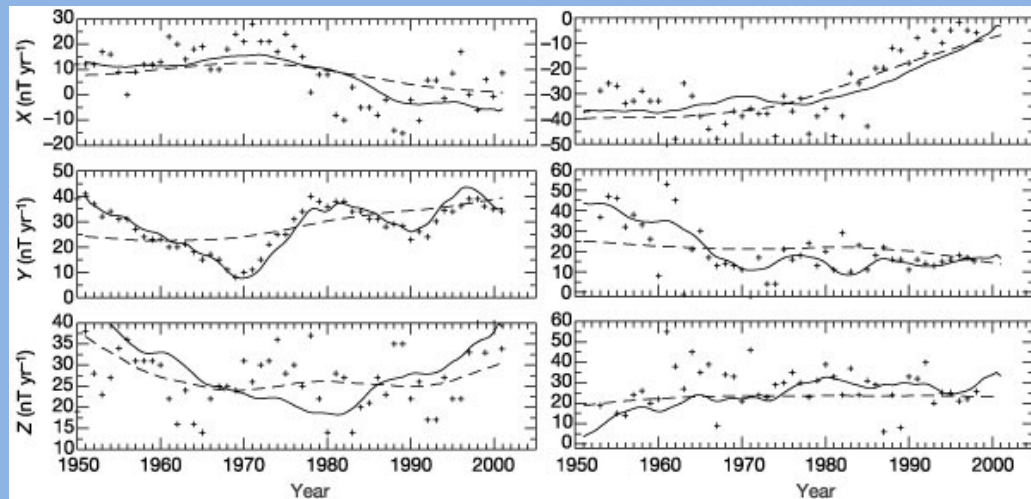
University of Liverpool

- Non-symmetry of fields of Uranus and Neptune
- Magnetic field and secular variation of Jupiter
- Geomagnetic secular variation spectrum
- **Stable stratification and waves at the top of the Core**
- Palaeointensity and inner core nucleation

# Stable Stratification and Secular Variation

Niemegk

Macquarie Island



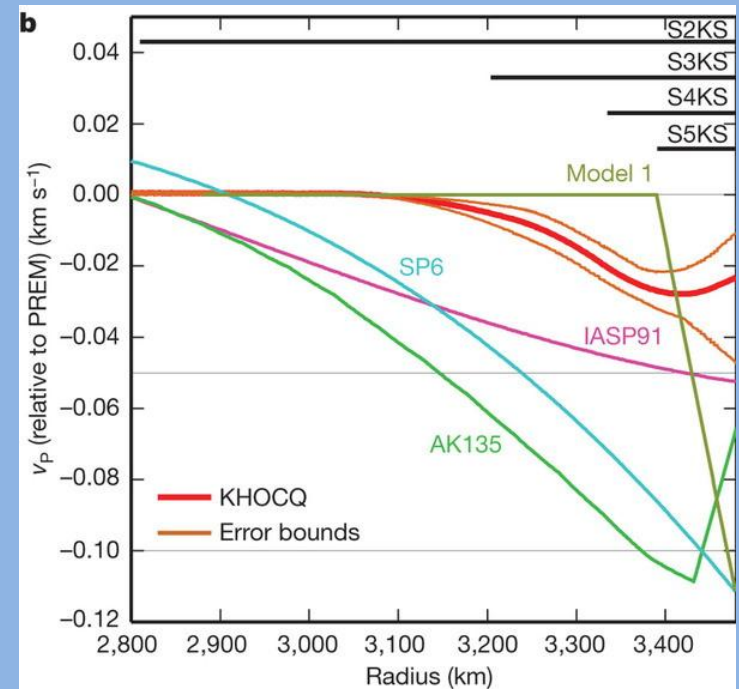
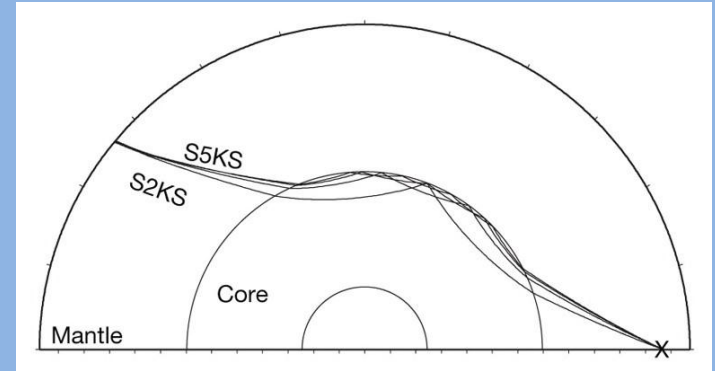
Dashed line — steady flow  
Solid line — + torsional oscillations

(Bloxham, Zatman and Dumberry, 2002)

- Torsional motions – zonal toroidal, equatorially symmetric - consistent with stable stratification and tangential geostrophy
- Steady flow cannot explain “geomagnetic jerk”, but additional torsional modes can do so
- Cannot explain other features of SV (including other jerks) – need more complex motions
- What other motions can be supported with stable stratification?

# Stable Stratification at top of Core

- Seismological evidence = Helffrich and Kaneshima argue for reduced seismic velocities near top of core
- Pozzo et al, 2012 – first principles calculations, increased thermal conductivity, BUT increased thermal conductivity :
- Zhang et al, 2015 – other first principles calculations suggest, “The presence of a stable layer, and the effects associated with an increased electrical conductivity, have significant implications for the geodynamo.”
- Seismological evidence of the stable stratification implies geomagnetic secular variation.”



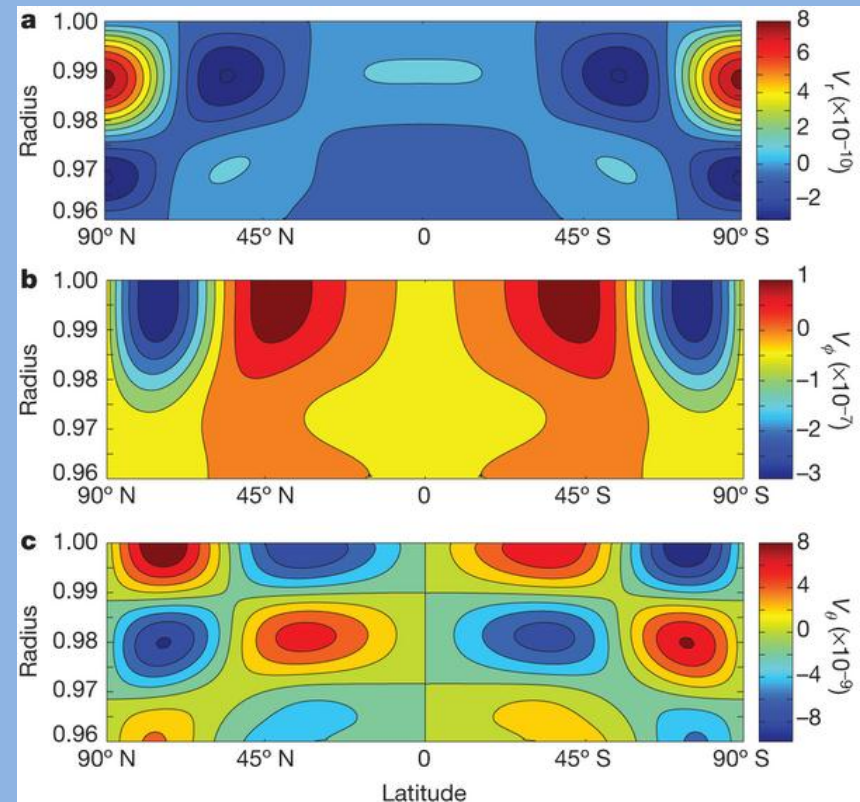
# Stable Stratification?

Buffett (2014) – evidence of MAC waves in time dependent zonal toroidal flow

Linear superposition of waves can account for  $V_\phi$

Makes predictions for  $V_\theta$

Flow zonal toroidal *and* poloidal



Model of MAC wave



# Stable Stratification?

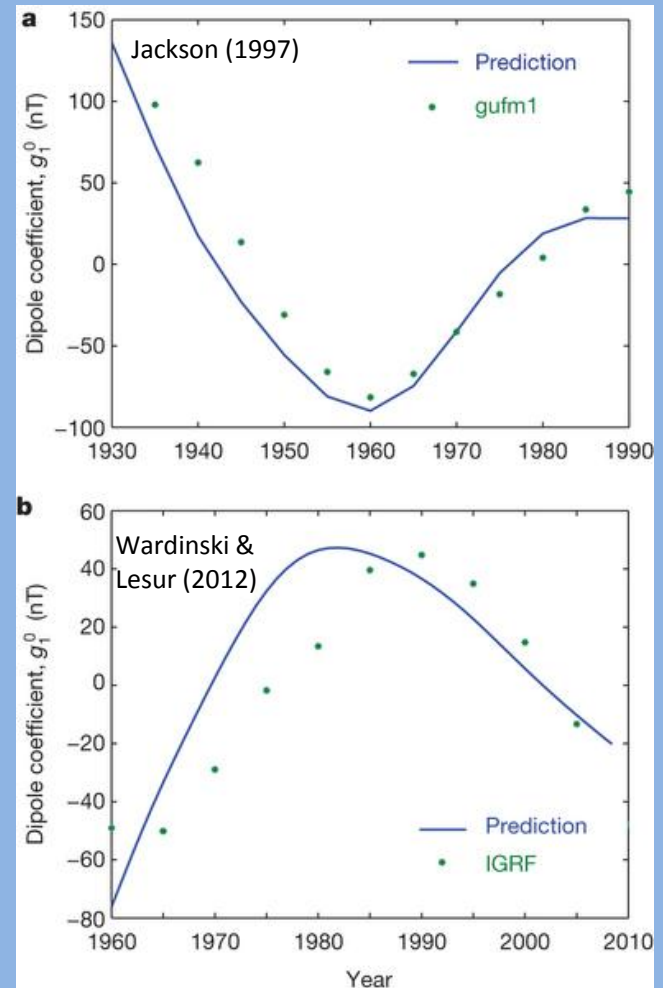
Buffett (2014) – evidence of MAC waves in time dependent zonal toroidal flow from 1930-1990

Linear superposition of waves can account for  $V_\phi$

Makes predictions for  $V_\theta$

Dipole field variation

- Explained for 1930-1990
- *Predicted* for 1960-2010



dipole fluctuations

# Core Flow Modelling

Radial component of induction equation  
(frozen-flux approximation)

$$\frac{\partial B_r}{\partial t} + \nabla_H (B_r \mathbf{u}) = 0$$

Flow obtained by inverting observed secular variation.

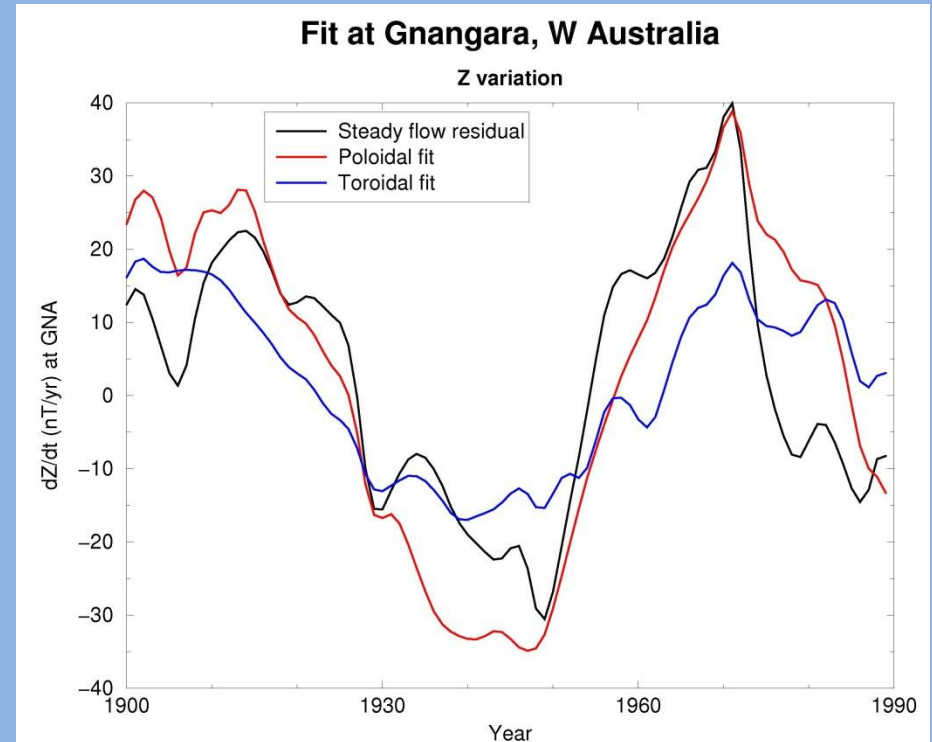
Additional assumptions needed to reduce non-uniqueness. Standard:

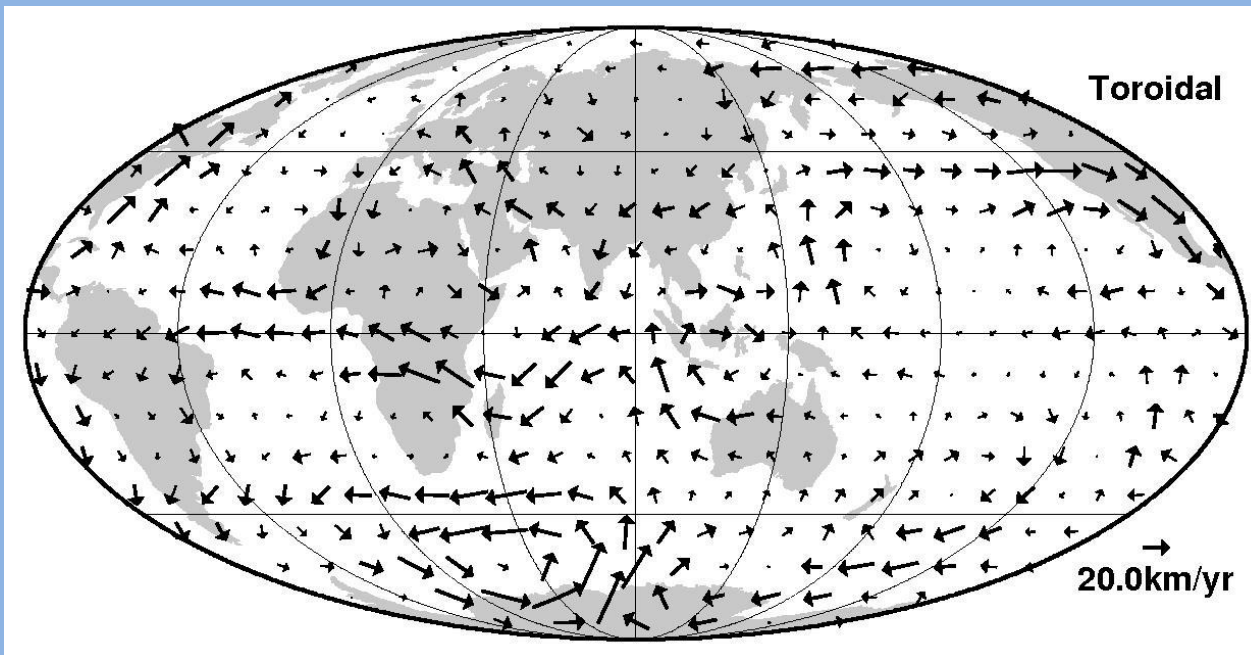
- steady
  - purely toroidal
  - tangentially geostrophic
- } no zonal poloidal flow

BUT: MAC wave solution has a time varying zonal flow with both toroidal *and poloidal* flows

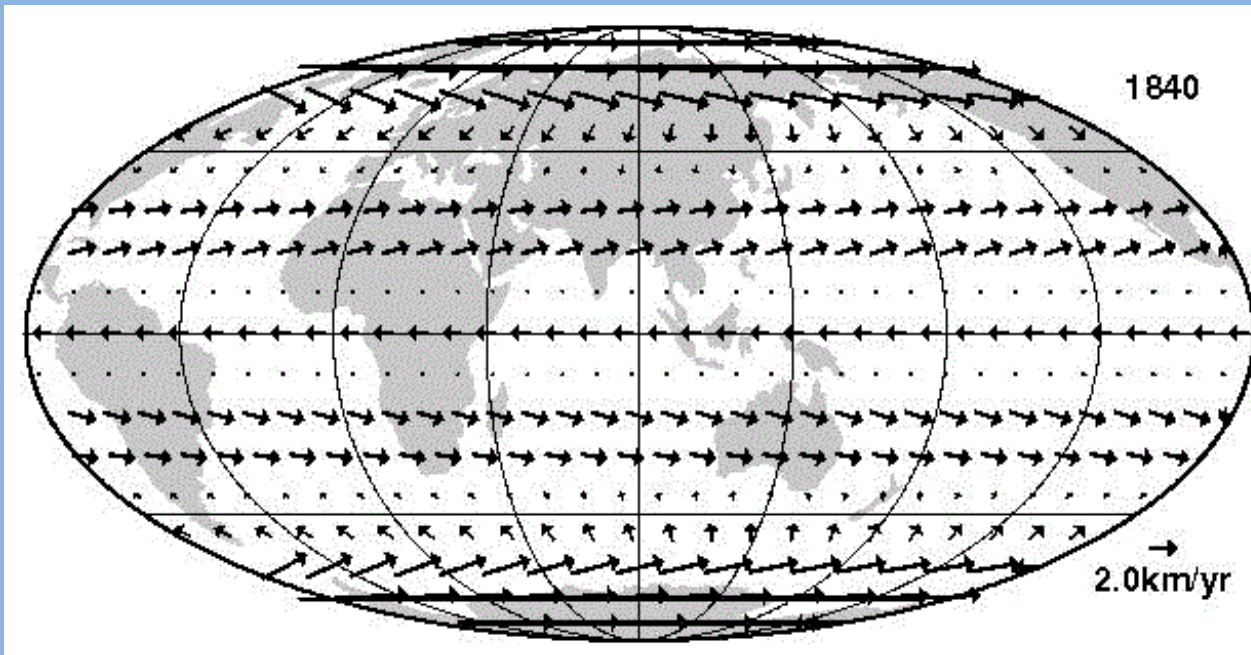
# New Flow Modelling

- Recover a constant toroidal steady flow
- Seek time varying flows to account for residual SV
  - Zonal
  - Equatorially symmetric
  - Toroidal, or toroidal and poloidal
- Including poloidal flows explains much additional SV (southern hemisphere geomagnetic jerks)





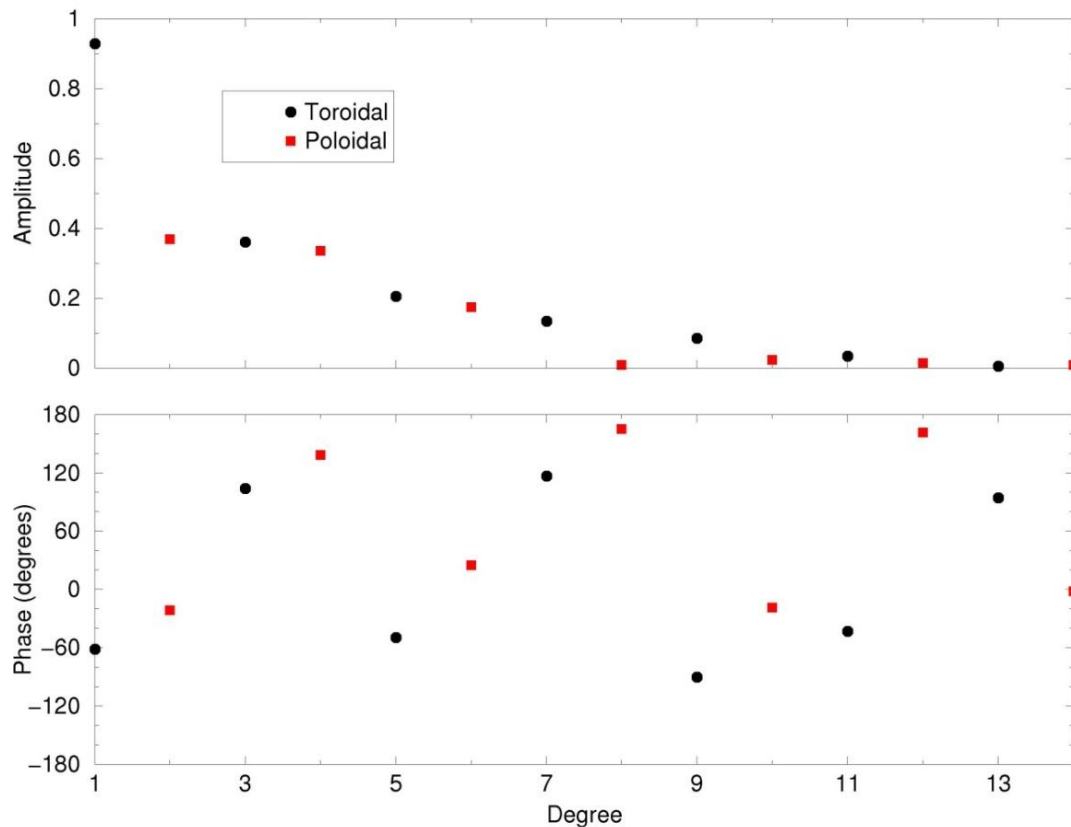
Steady  
toroidal  
flow



Time  
varying  
component

# Wave fit to different components

Amplitude and Phase of 50-year waves



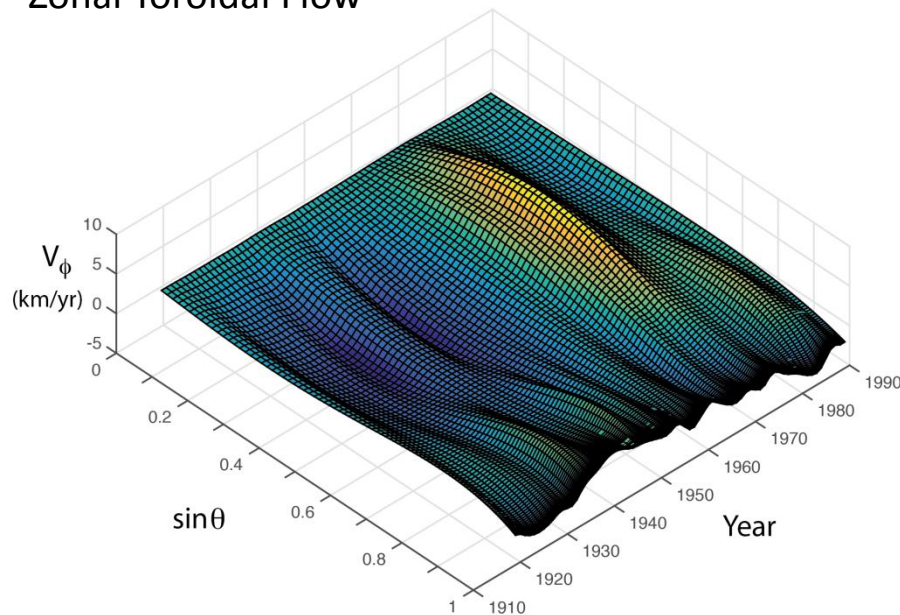
- Fit sine waves to different flow modes
- Best common fit at  $T \approx 50$  years
- Fall in amplitude with complexity
- Structure in phase difference between toroidal and poloidal components

Similar behavior expected for MAC waves

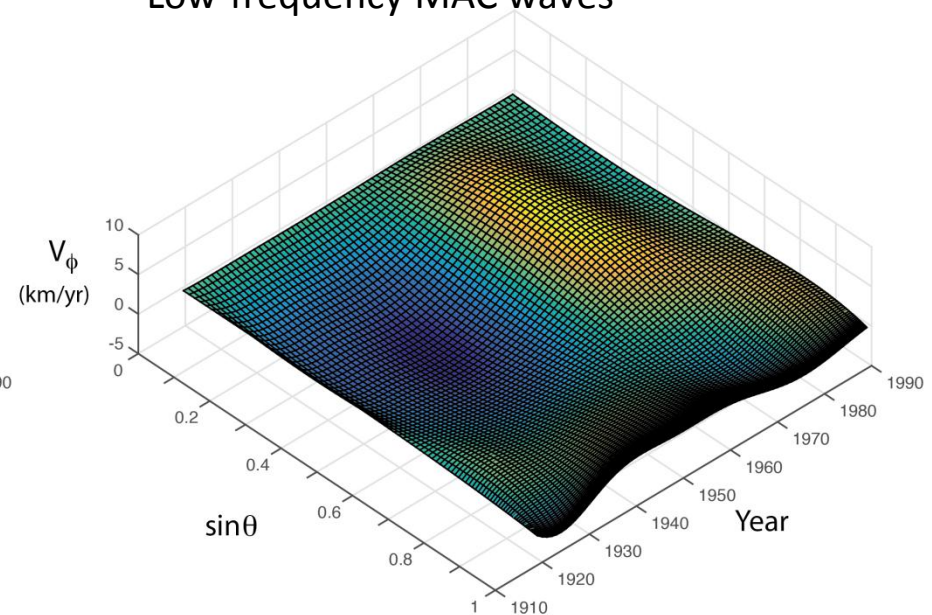
# Linking theory and observations

Fit MAC waves to zonal toroidal flow -> compare predictions for poloidal flow

Zonal Toroidal Flow



Low-frequency MAC waves



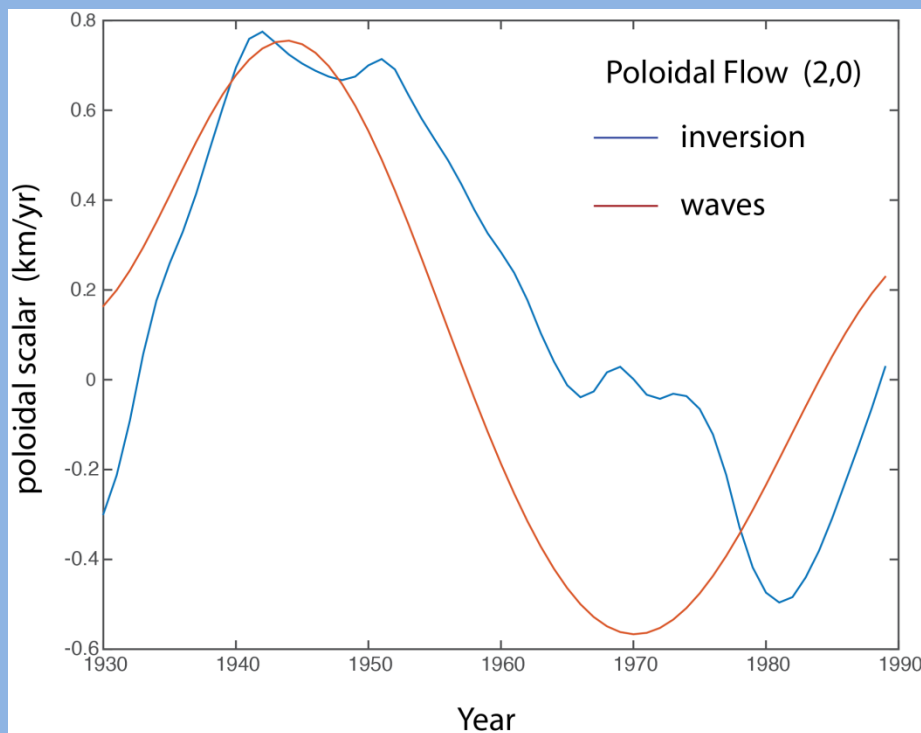
buoyancy frequency  $N \sim \Omega$



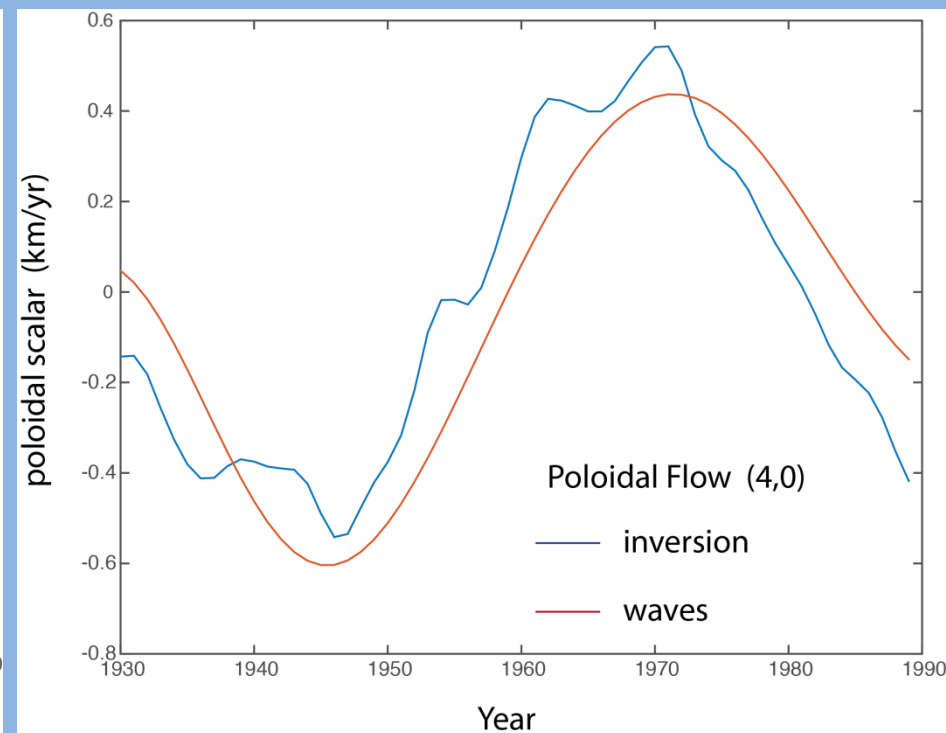
# Predicting Poloidal Flow

- Fit MAC waves to zonal toroidal flow
- -> predictions for poloidal flow fit observations

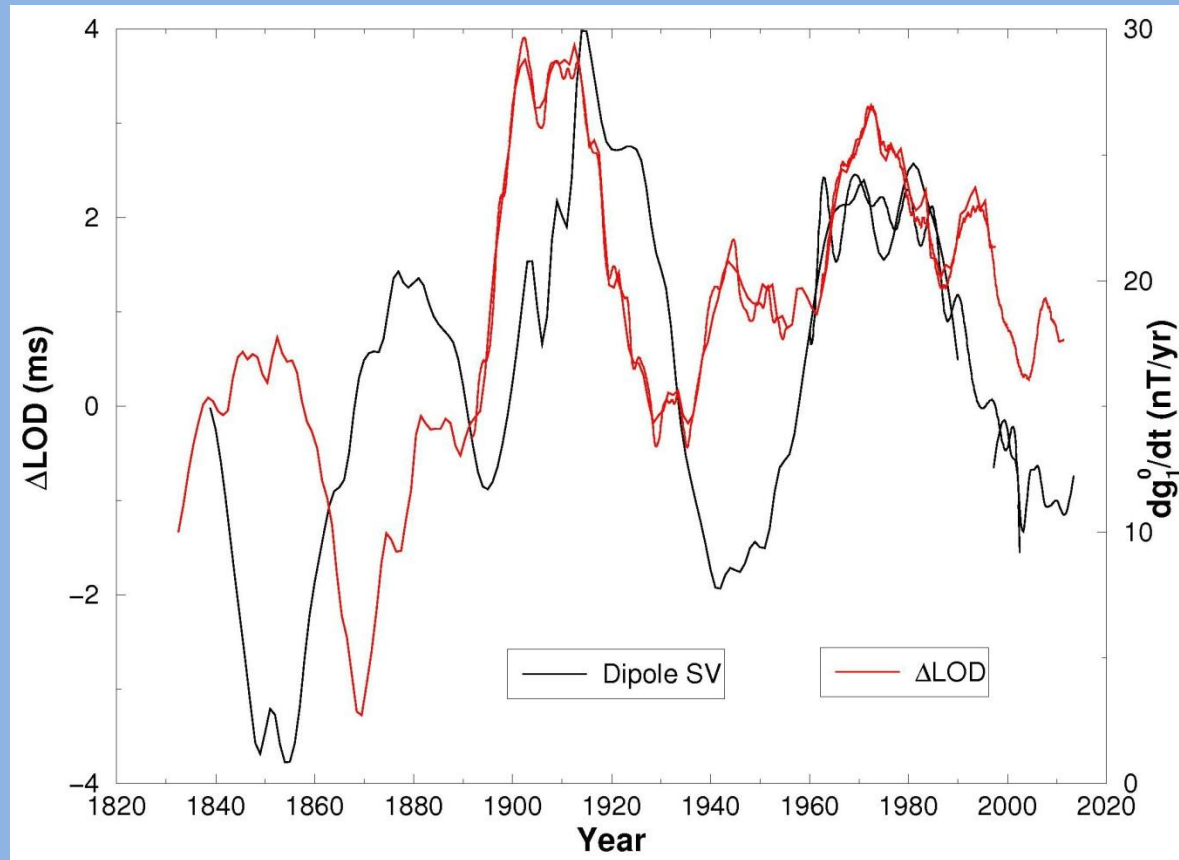
Degree 2



Degree 4



# Comparing $\Delta\text{LOD}$ and Axial Dipole SV



- Axial dipole and  $\Delta\text{LOD}$  both have “60yr” variation
- But zonal toroidal flows don’t give axial SV
- “Geomagnetic jerks” in axial SV – not from torsional oscillations
- This is either profoundly important or completely irrelevant!

# Observational Constraints on Planetary Dynamos

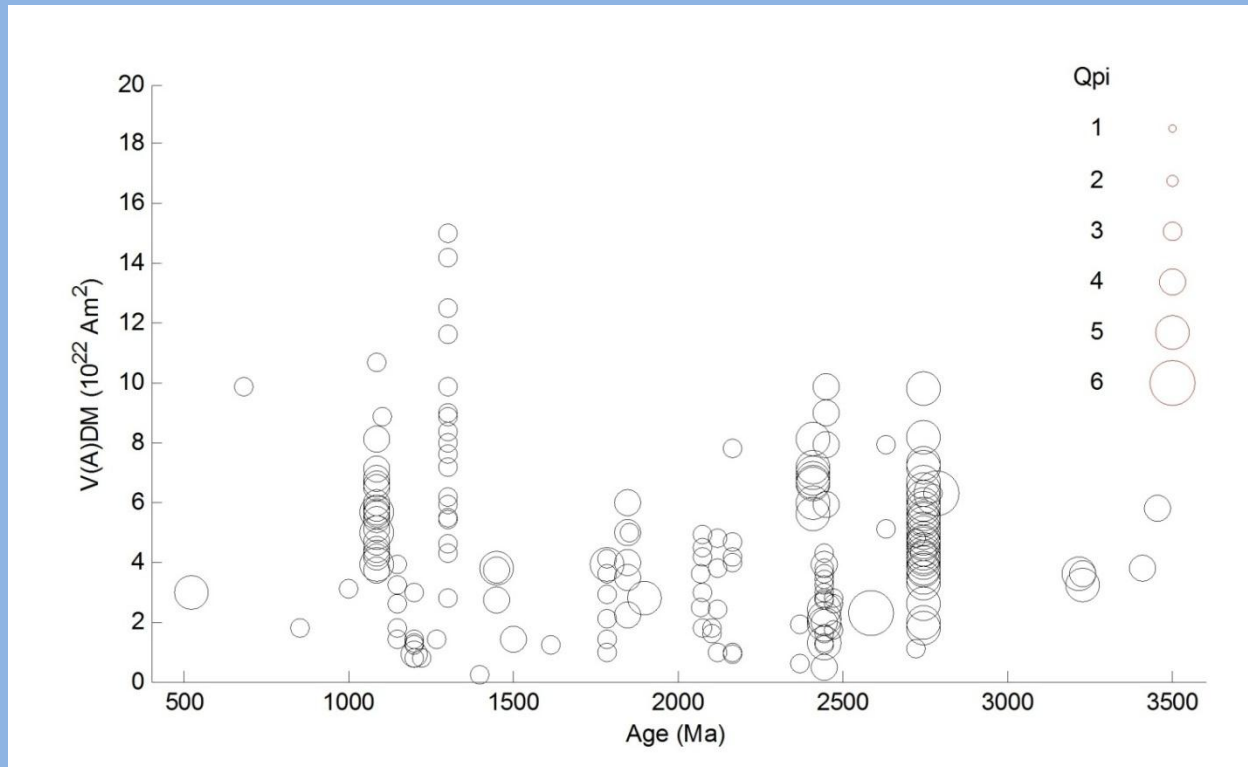
Richard Holme

University of Liverpool

- Non-symmetry of fields of Uranus and Neptune
- Magnetic field and secular variation of Jupiter
- Geomagnetic secular variation spectrum
- Stable stratification and waves at the top of the Core
- Palaeointensity and inner core nucleation

# Implications for Inner Core Growth

- Dipole moment from very old palaeointensity results
  - more reliable data  $\Leftarrow$  larger symbols (Biggin et al 2015)



- Consistent with inner core origin approx. 1.4 Byr ago
- Easier to explain with traditional core conductivity
- Seismological evidence still implies stable stratification

# Conclusions

- Non-symmetry of fields of Uranus and Neptune
  - Treat data from models
- Magnetic field and secular variation of Jupiter
  - Perhaps more can be extracted from observations
  - Juno will test this!
- Geomagnetic secular variation spectrum
  - Very clean relation to test against dynamo models
- Stable stratification and waves at the top of the Core
  - Beware of getting too caught up in one “school” (QG)
- Palaeointensity and inner core initiation
  - Perhaps the “New Normal” isn’t.....