

Radial Differential Rotation of Sun-like stars

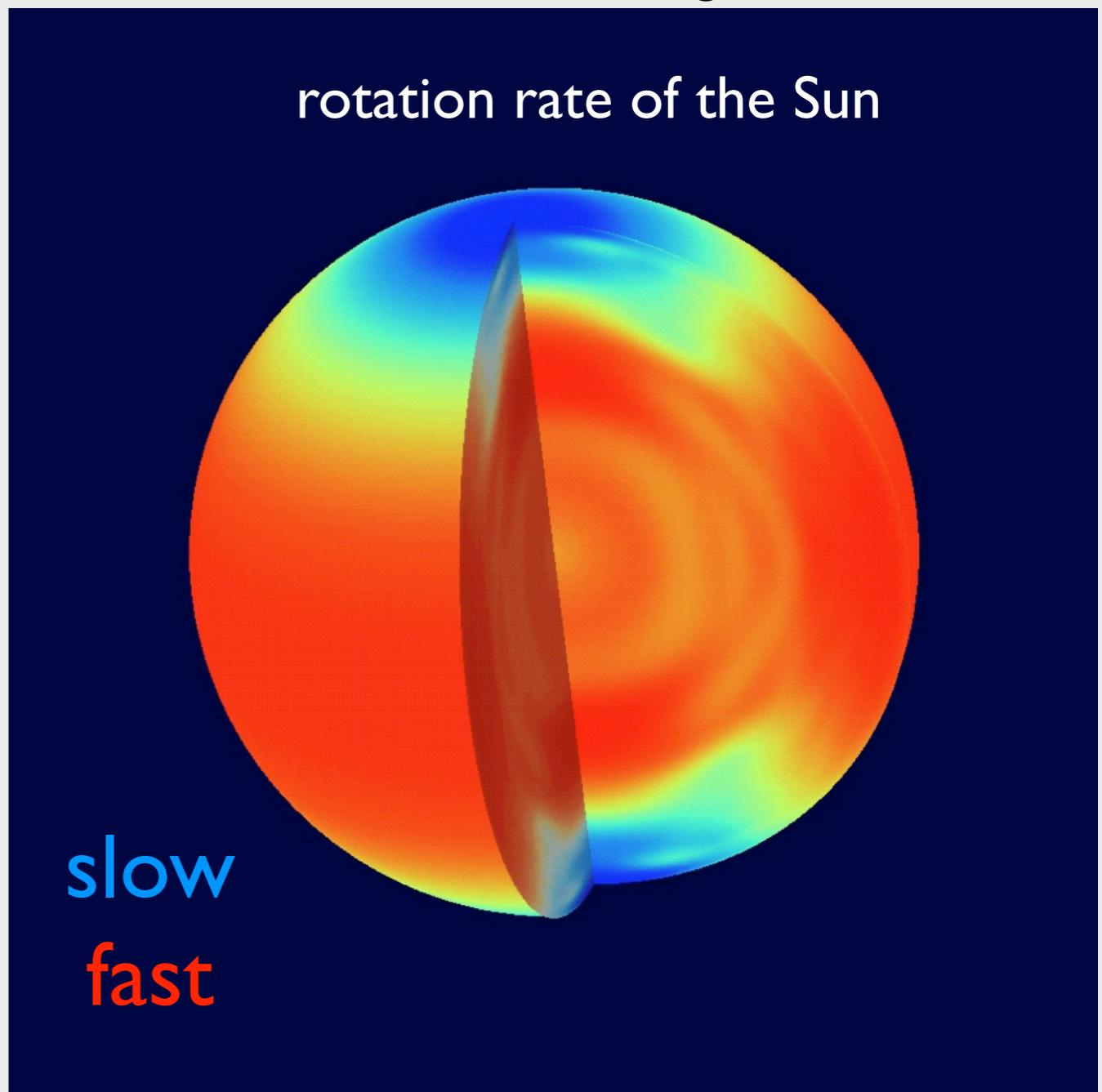
Hannah Schunker
Jesper Schou & Warrick Ball

Martin Bo Nielsen

Rotation and Activity

- Stars are magnetically active
- Magnetic field is generated in the interior (dynamo)
- Not well understood

$$P_{\odot} \approx 27 \text{ days}$$

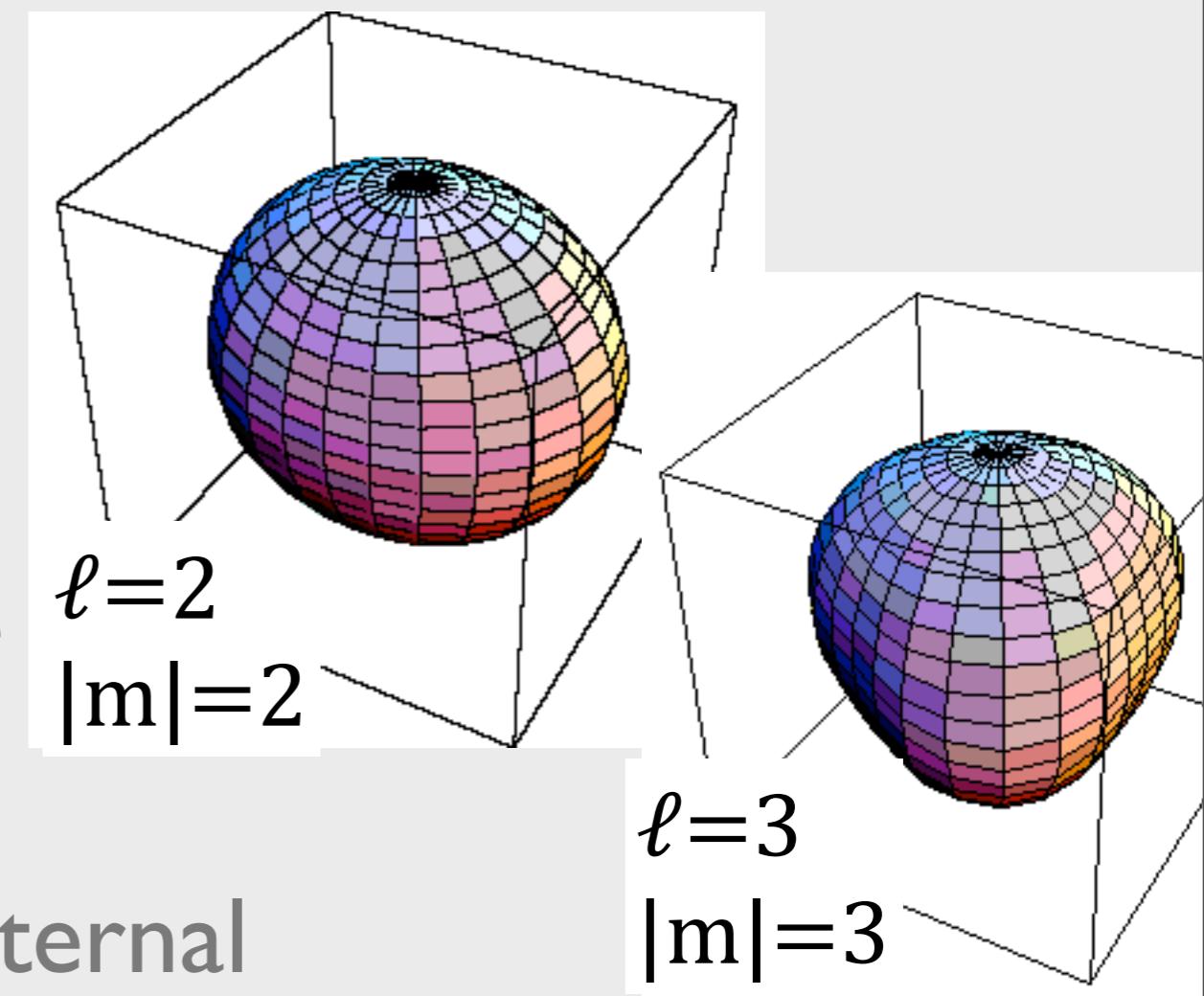


Schou et al 1998

H. Schunker

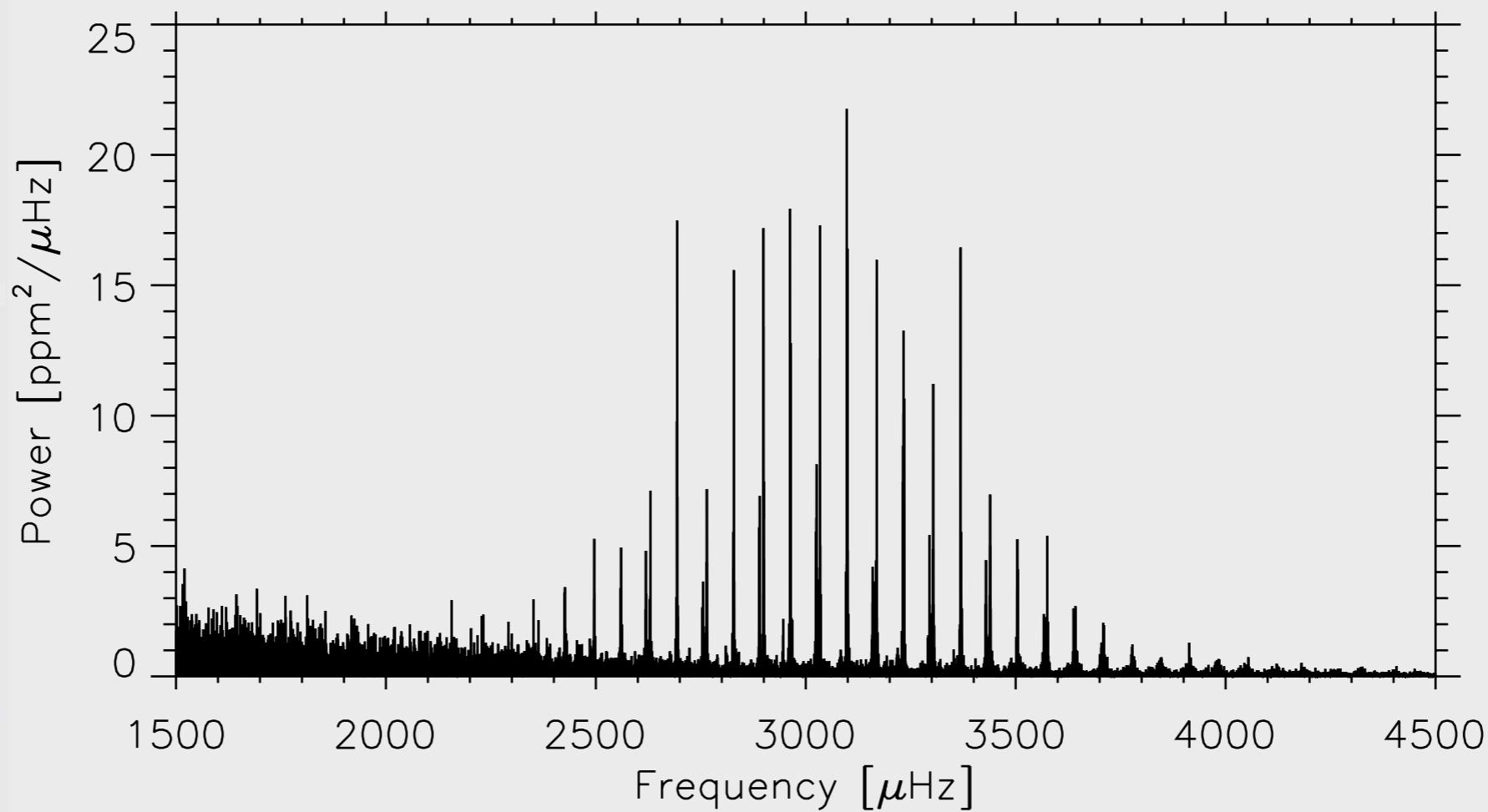
Tool: Asteroseismology

- Solar-like oscillations are stochastically excited by turbulent convection
- Spherical harmonics ℓ , harmonic degree m, azimuthal order n, radial order
- Oscillations sensitive to interior
- Inversions to infer internal structure & rotation



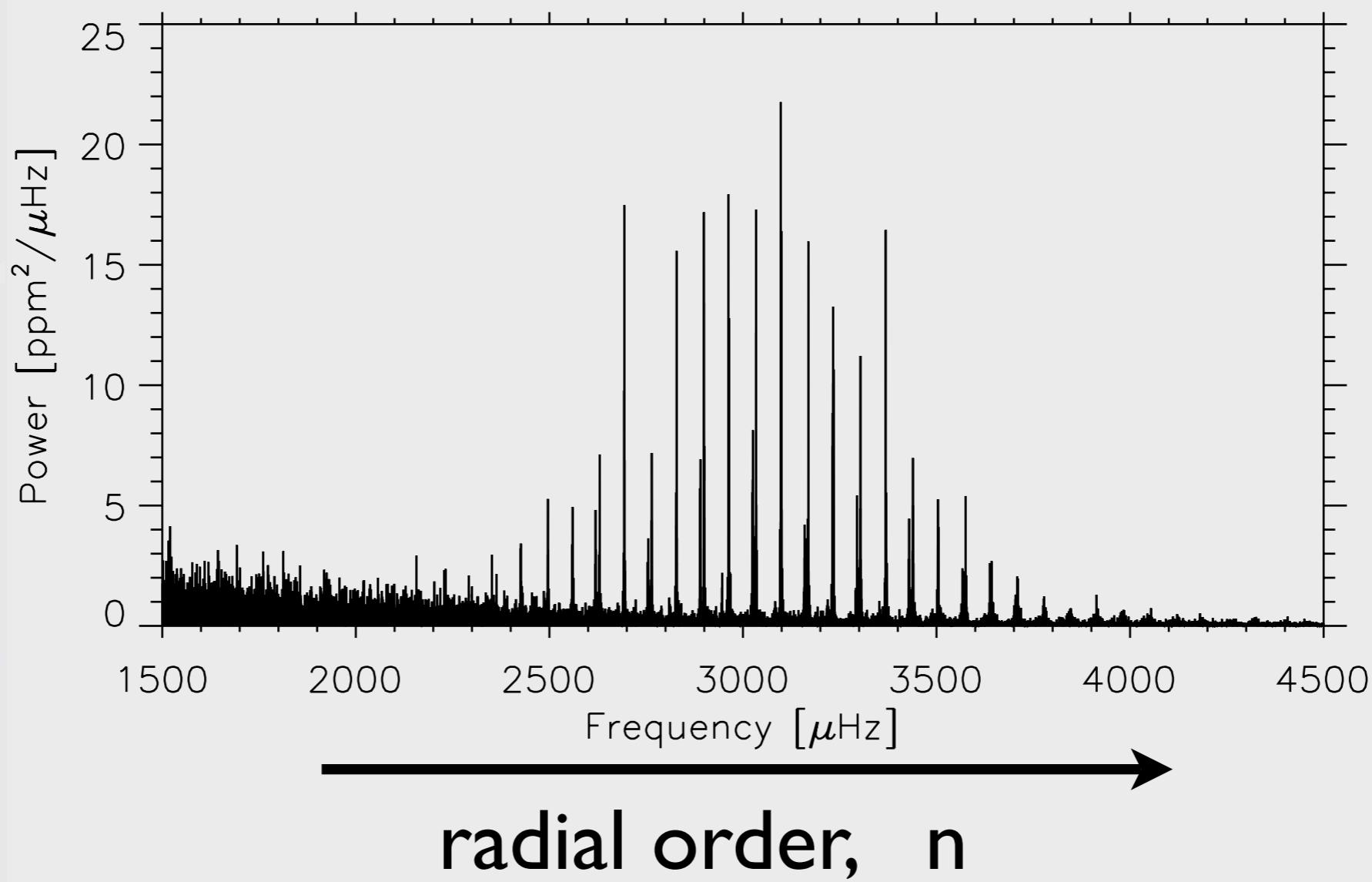
Tool: Asteroseismology

- Observe light curve or Doppler velocity as a function of time
- Measure properties of the power spectrum



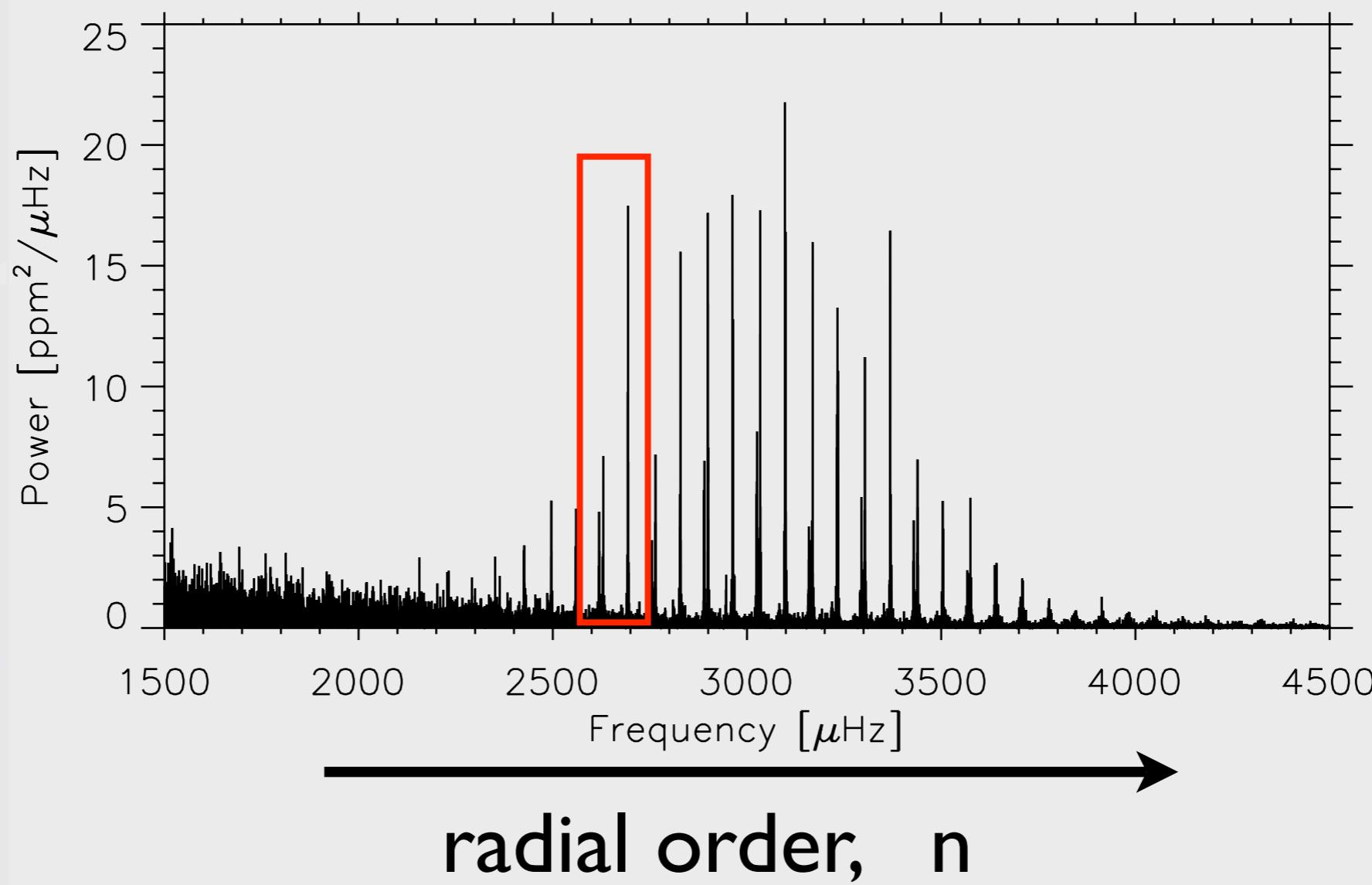
Tool: Asteroseismology

- Observe light curve or Doppler velocity as a function of time
- Measure properties of the power spectrum

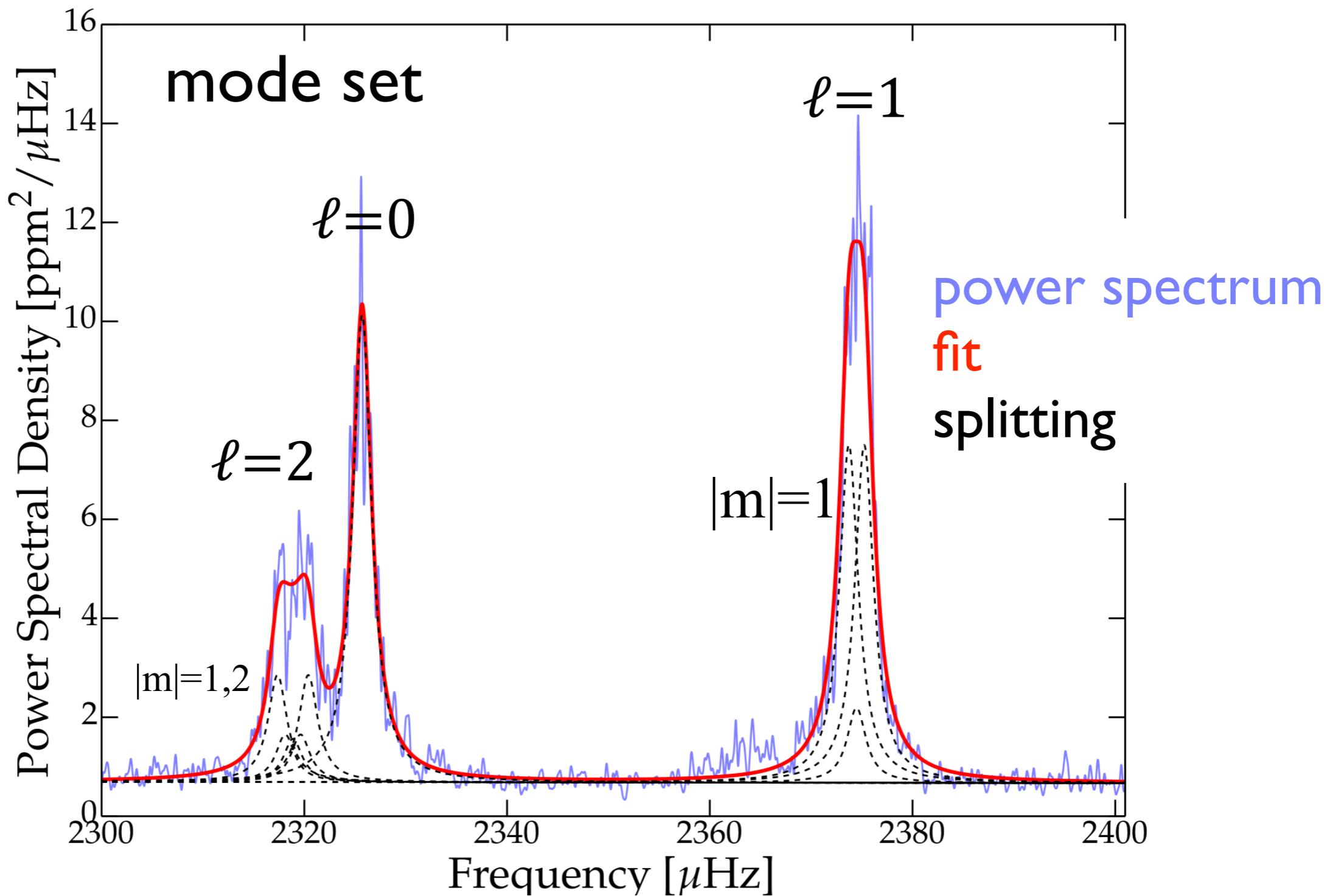


Tool: Asteroseismology

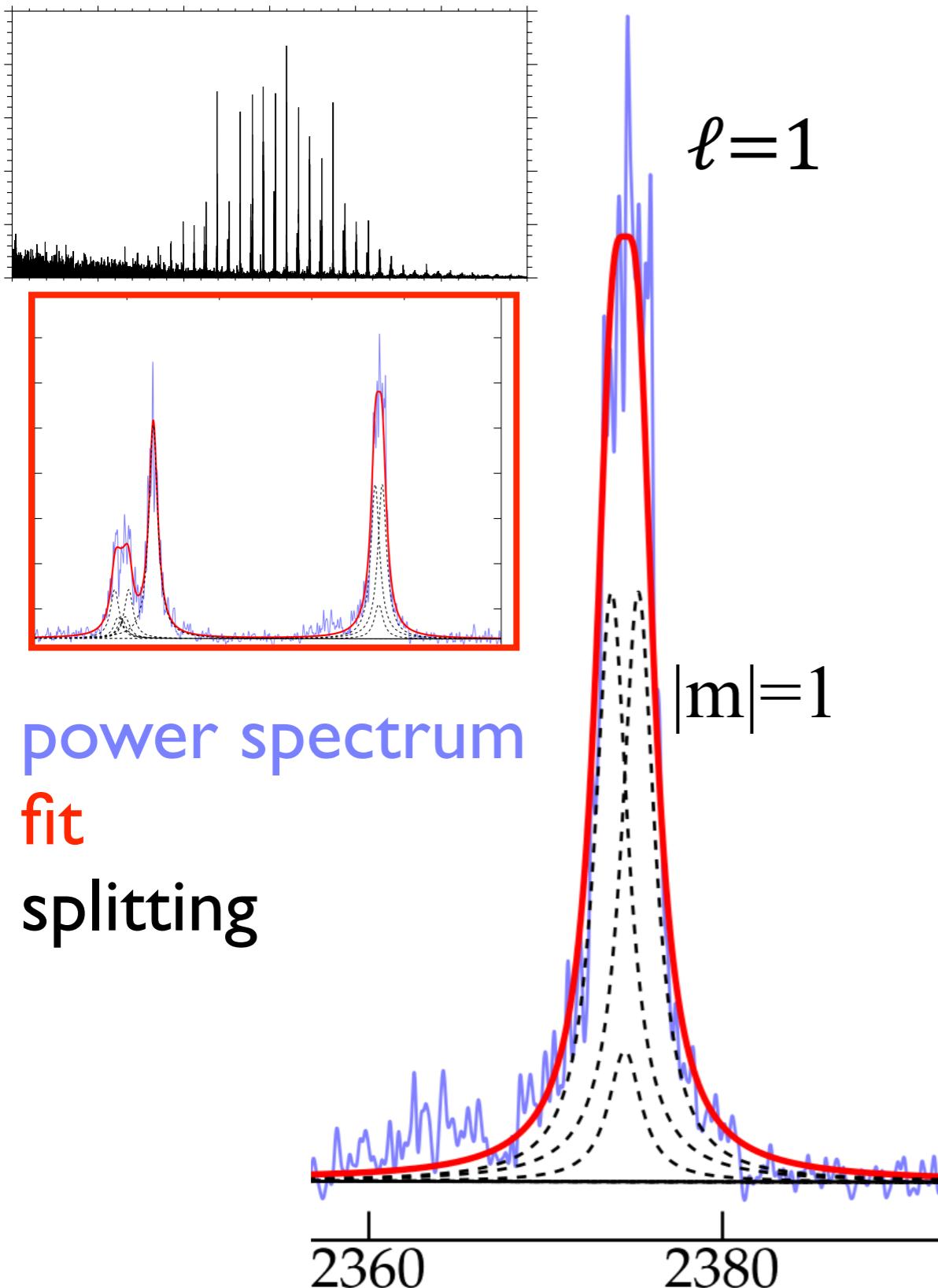
- Observe light curve or Doppler velocity as a function of time
- Measure properties of the power spectrum



Tool: Asteroseismology



Tool: Asteroseismology



- Measure rotational splittings of the modes

m , azimuthal order:
splittings
 n , radial order:
depth sensitivity

Inversions for Interior Rotation

observed

$$\delta\omega_i = \int_0^R K_i(r)\Omega(r)dr + \sigma(\delta\omega_i)$$

from stellar models

uncertainty in
observations



Inversions for Interior Rotation

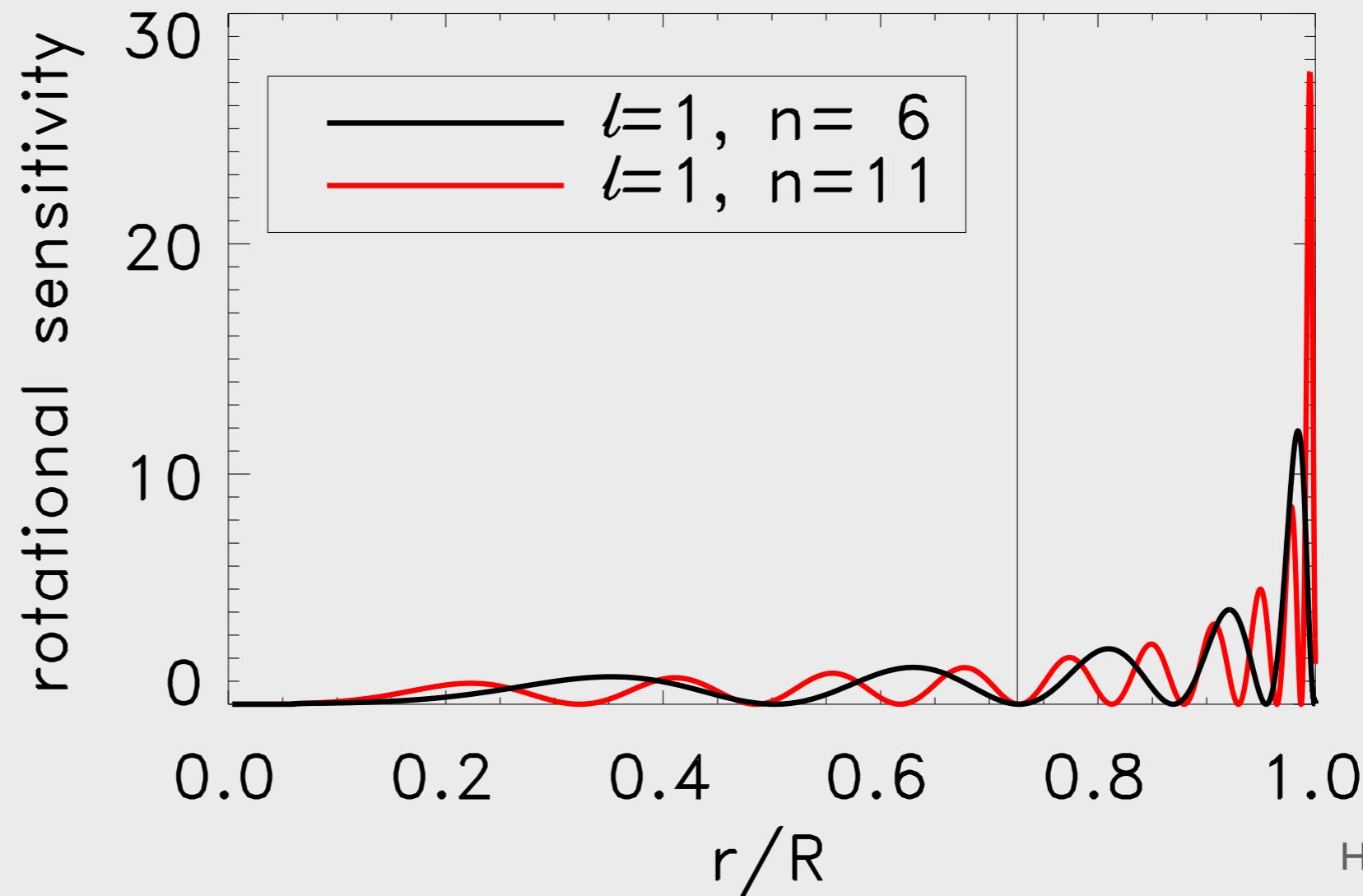
observed 

$$\delta\omega_i = \int_0^R K_i(r)\Omega(r)dr + \sigma(\delta\omega_i)$$

from stellar models 

? 

uncertainty in observations 



Inversions for Interior Rotation

observed

$$\delta\omega_i = \int_0^R K_i(r)\Omega(r)dr + \sigma(\delta\omega_i)$$

?

from stellar models

uncertainty in
observations

- To solve: Regularised Least Squares (RLS) inversions

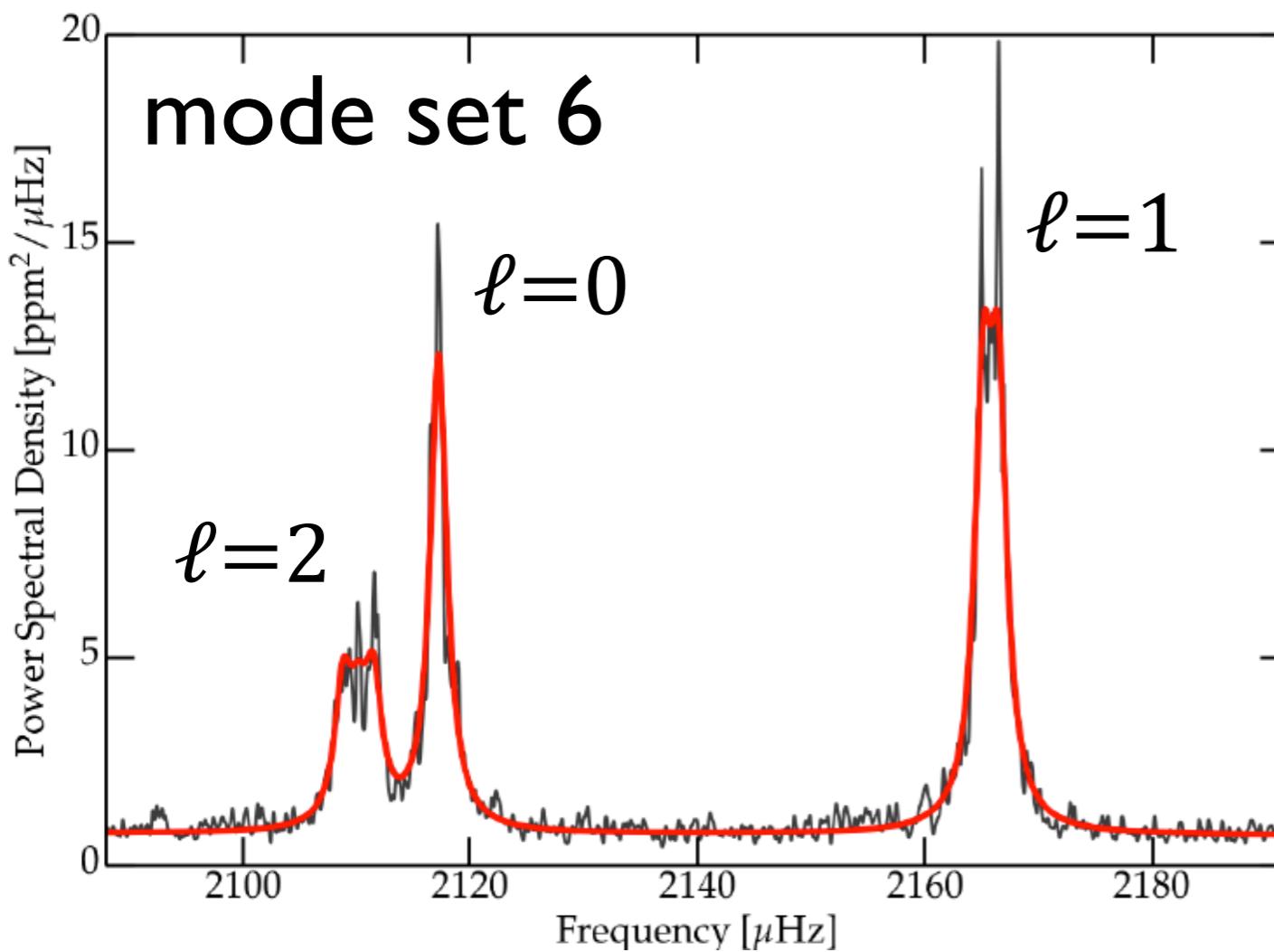
Minimise

$$\sum_{i=1}^M \left[\delta\omega_i - \int_0^R \mathcal{K}_i(r)\bar{\Omega}(r)dr \right]^2 + \text{smoothing}$$

Rotation in Six Sun-like stars

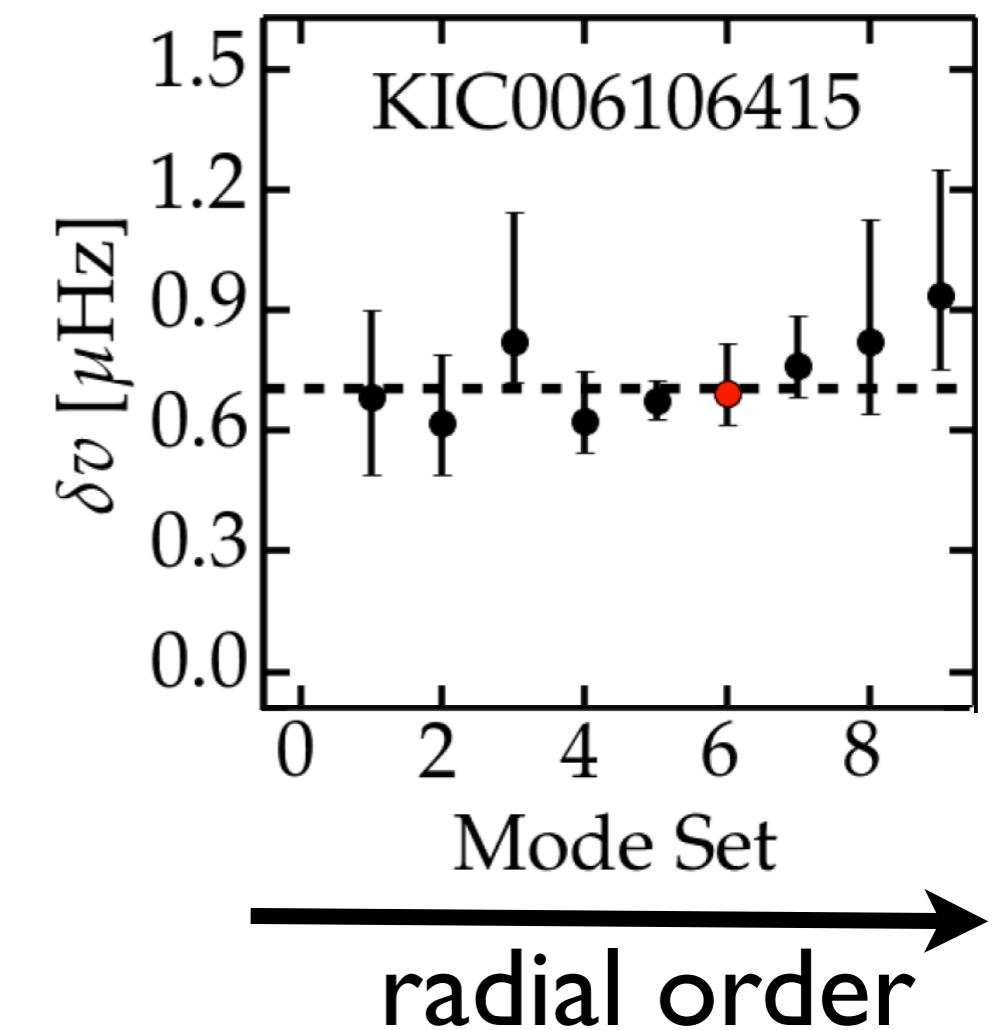
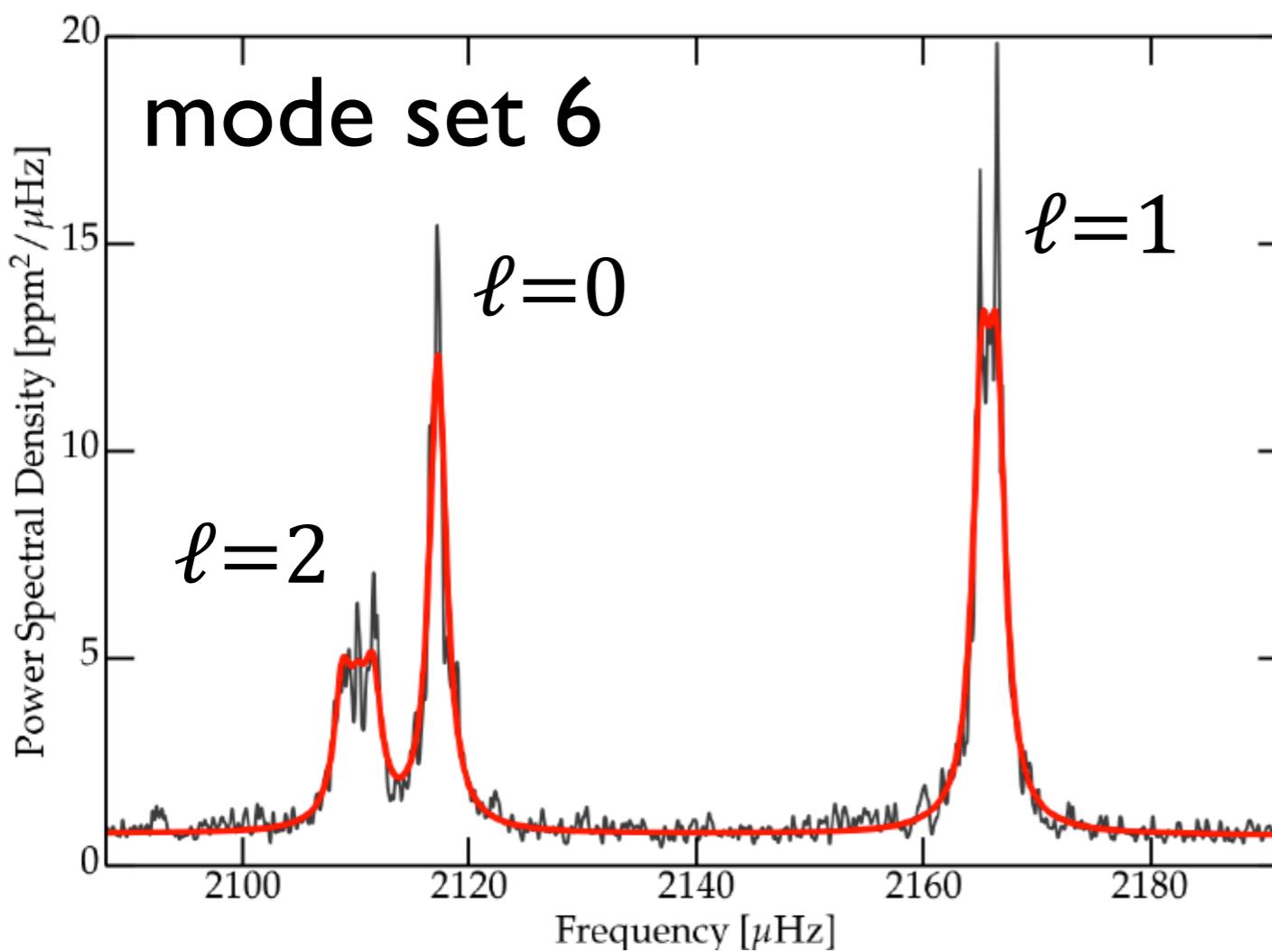
- Kepler observed many stars suitable for asteroseismology over four years
- We identified six Sun-like stars with excellent power spectra and visible signs of rotation *Nielsen et al 2014*
 $5600 \text{ K} < T < 6100 \text{ K}$
- Measured rotational splittings as a function of radial order, n

Rotation in Six Sun-like stars



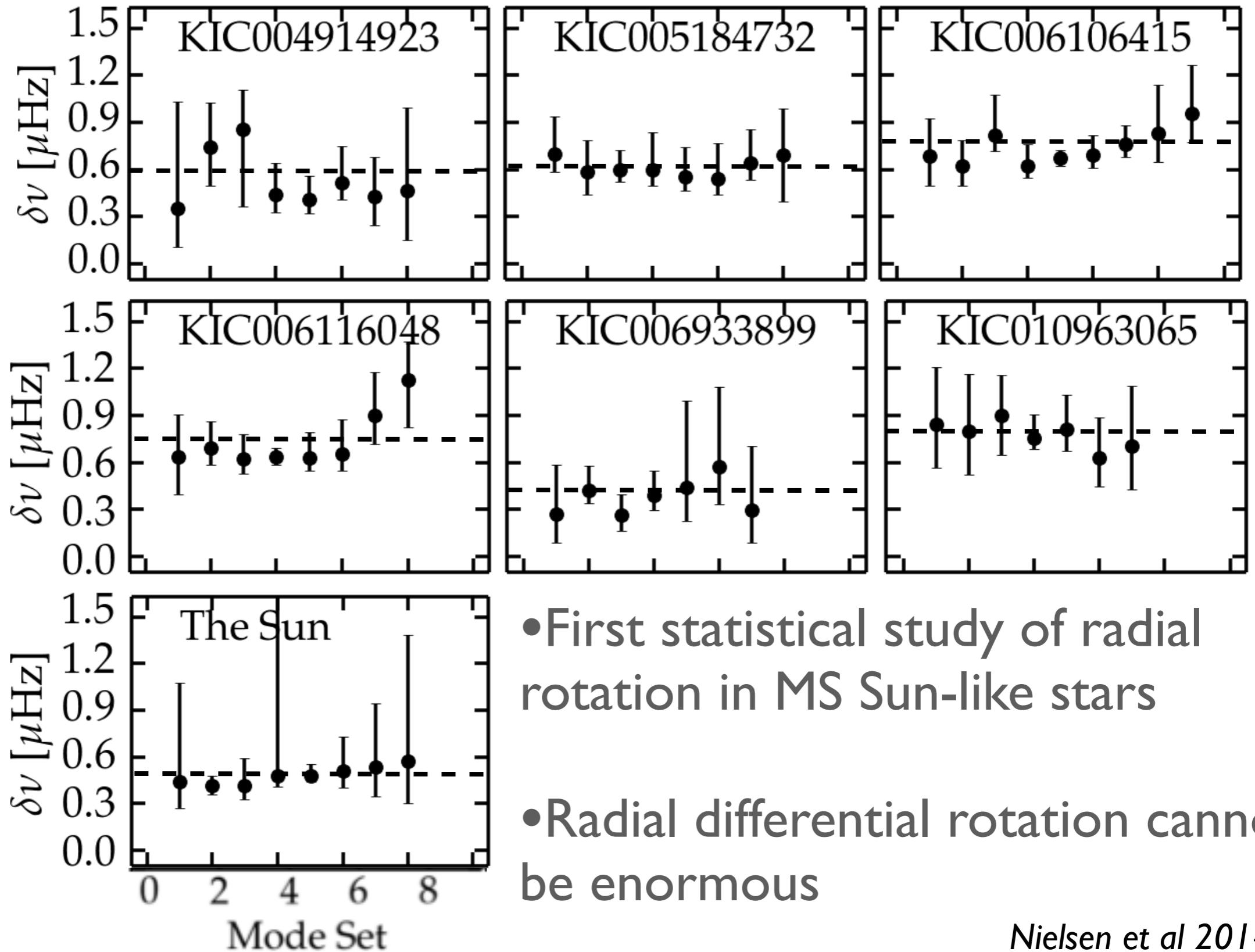
Nielsen et al 2014

Rotation in Six Sun-like stars

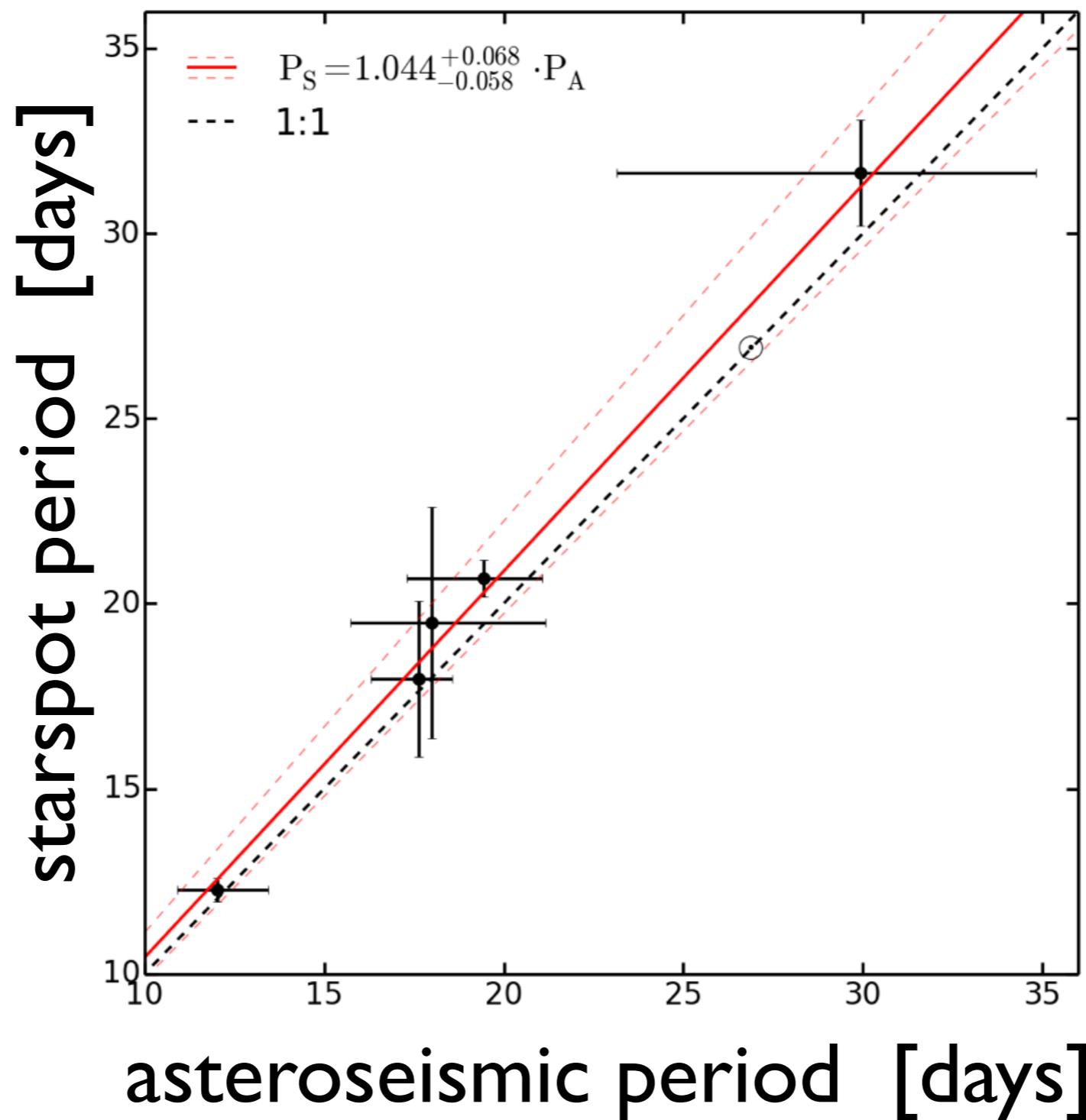


Nielsen et al 2014

Rotation in Six Sun-like stars



Rotation in Six Sun-like stars



See Martin Bo Nielsen's poster

Nielsen et al, submitted

H. Schunker

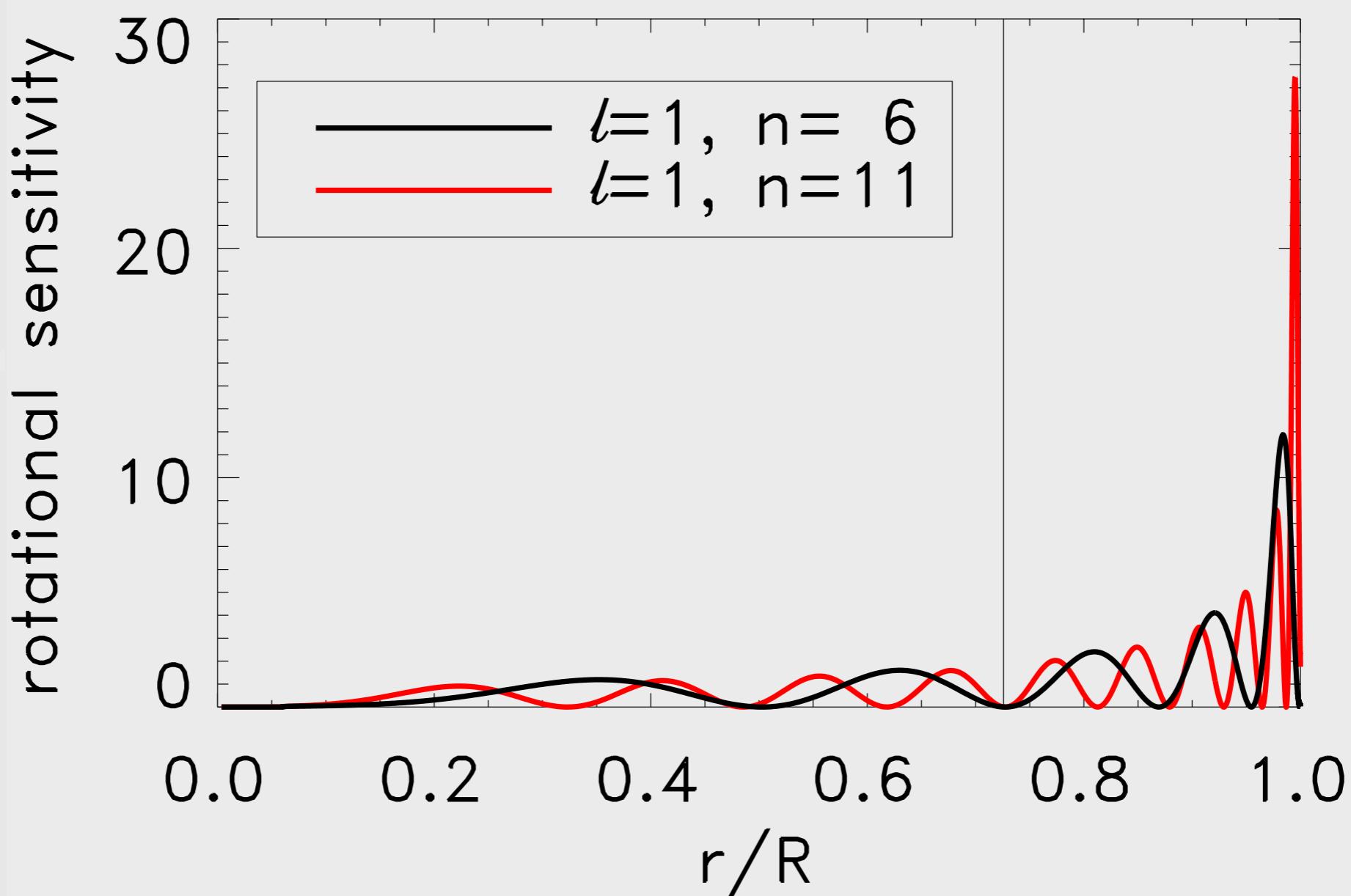


Can we invert for these stars and extract useful information?

Radial Differential Rotation of Sun-like Star

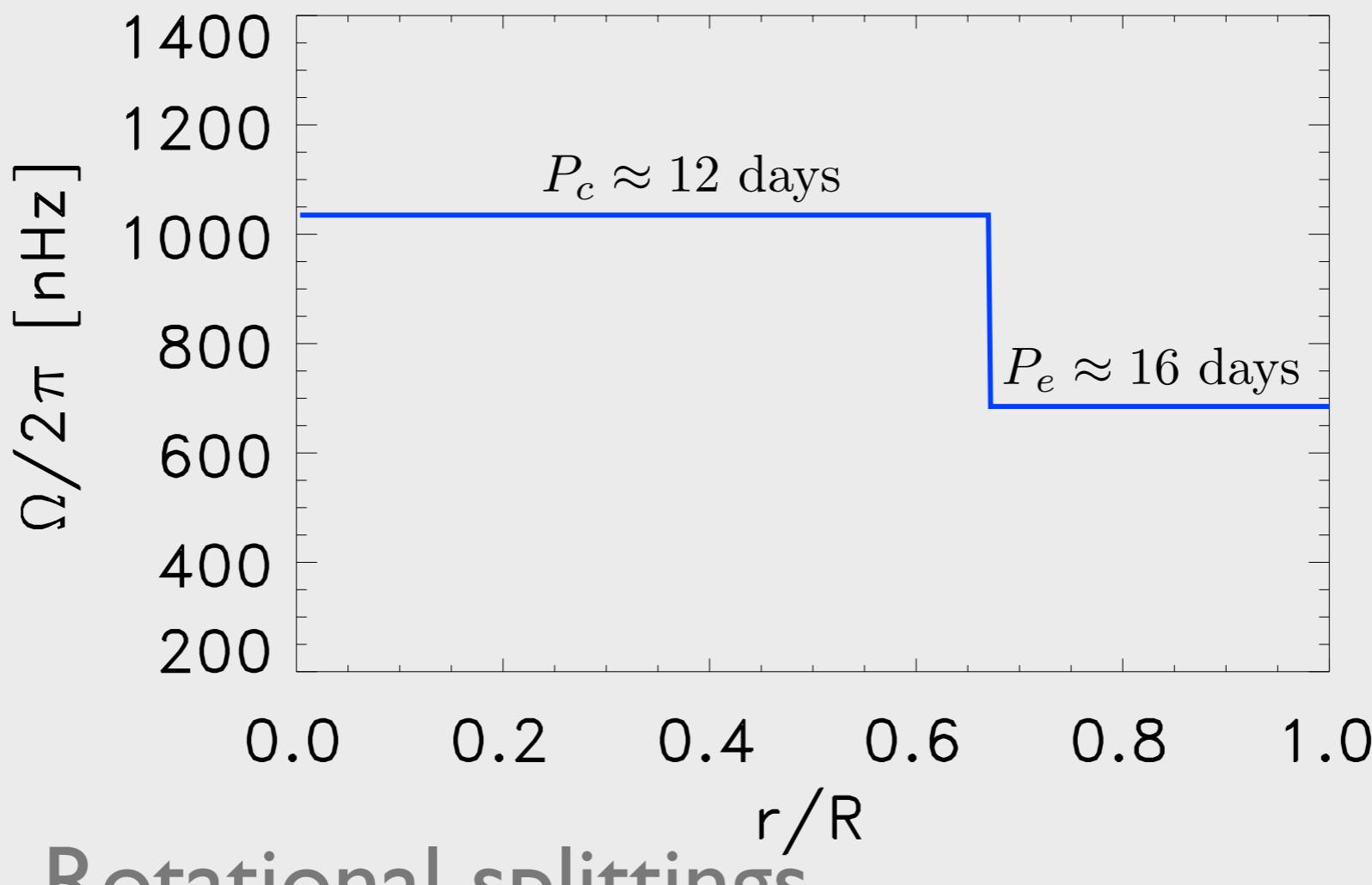
- Stellar model of main sequence Sun-like star

$M/M_{\odot} = 1.1$ $\text{Fe/H} = 0.5$ $\text{BCZ} = 0.672R_{\star}$ $\text{Teff} = 5640 \text{ K}$



Radial Differential Rotation of Sun-like Star

- Synthetic rotation profile



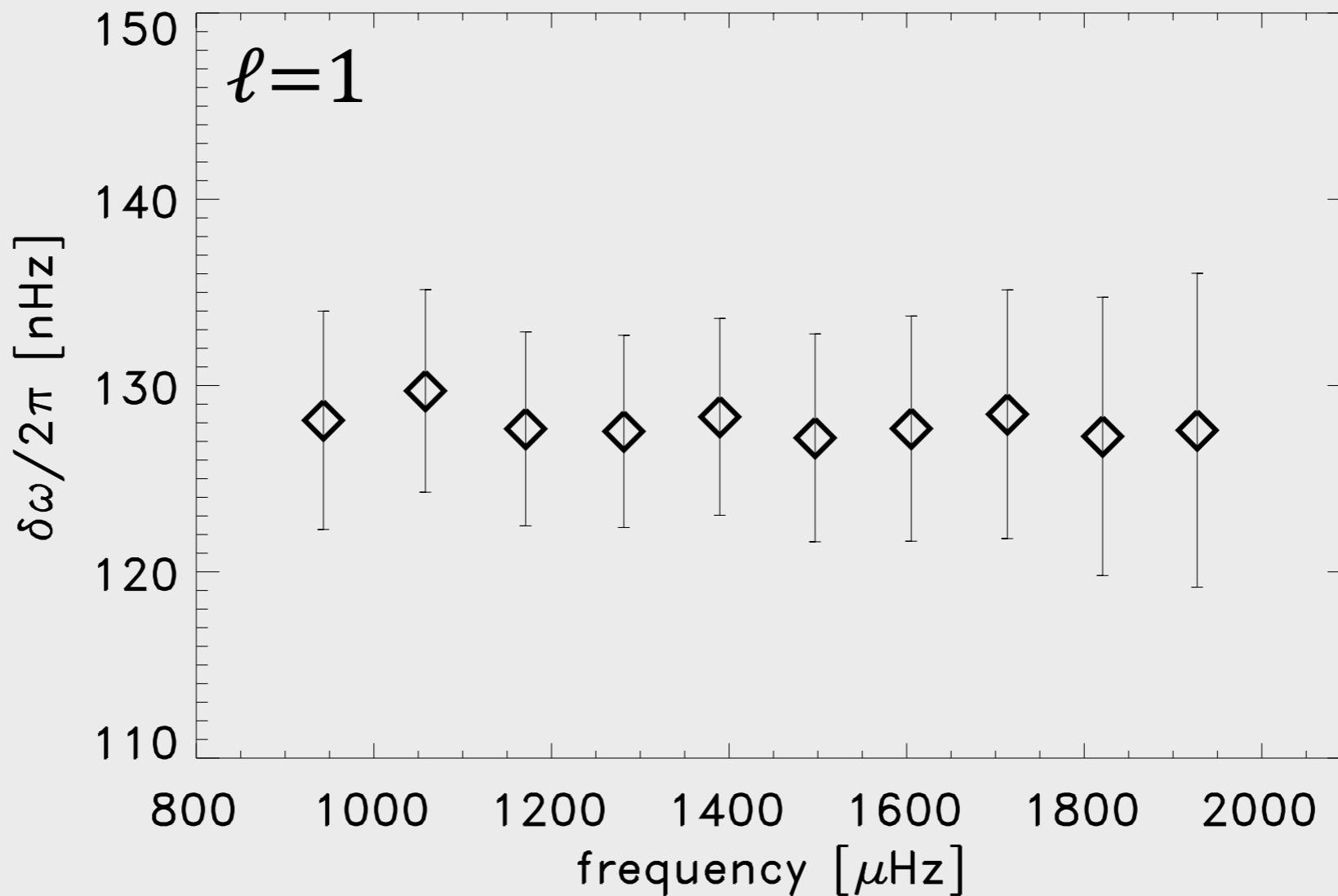
- Rotational splittings

$$\delta\omega_i = \int_0^R K_i(r) \Omega(r) dr + \sigma(\delta\omega_i)$$

Radial Differential Rotation of Sun-like Star

- Uncertainties on the splittings based on scaling relations from Sun

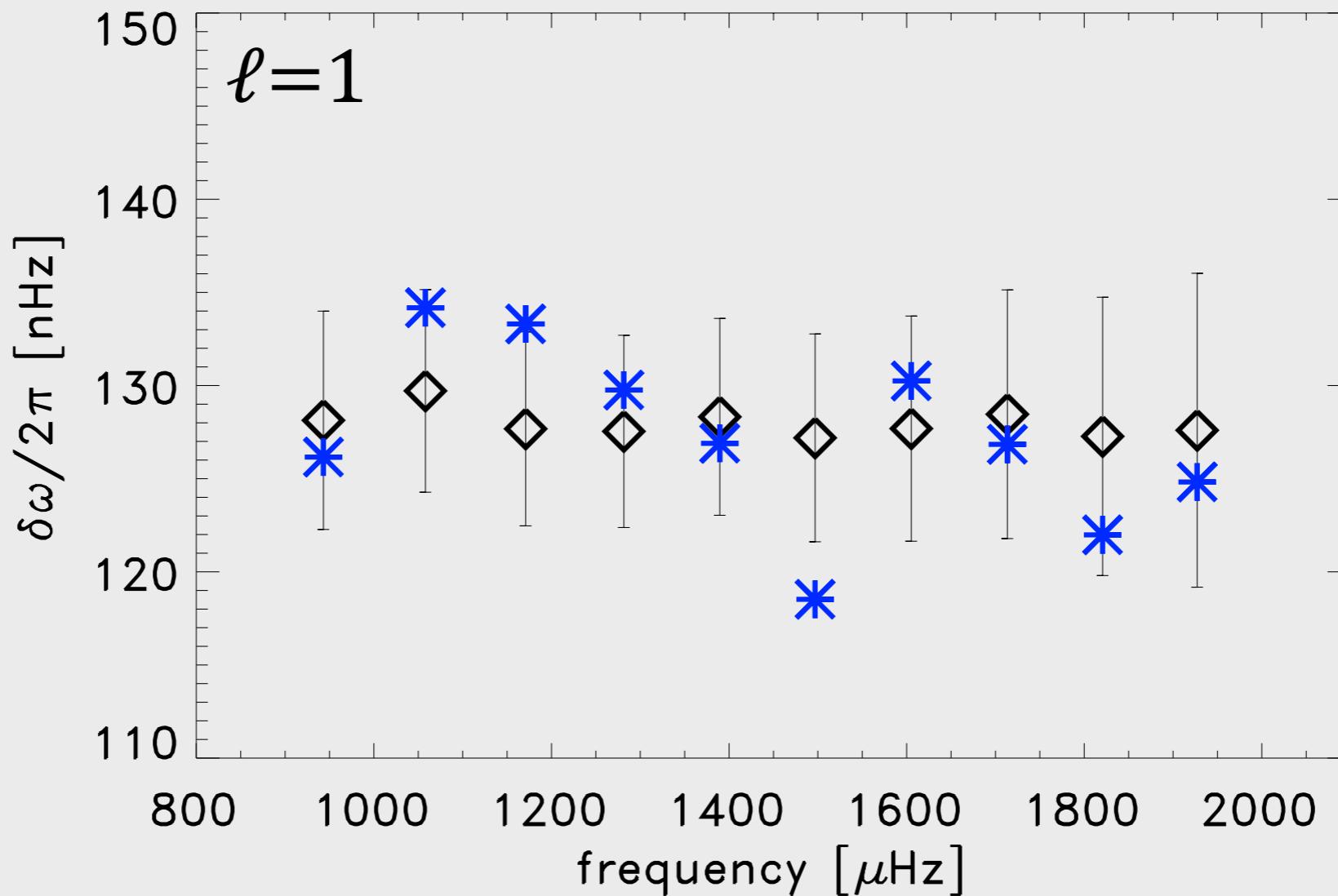
$$\sigma(\omega) = \sqrt{\frac{\Gamma}{4\pi T}} \rightarrow \sigma(\delta\omega) = \frac{\sigma(\omega)}{\sqrt{1/3\ell(\ell + 1)}}$$



Radial Differential Rotation of Sun-like Star

- Uncertainties on the splittings based on scaling from solar temperature

$$\sigma(\omega) = \sqrt{\frac{\Gamma}{4\pi T}} \rightarrow \sigma(\delta\omega) = \frac{\sigma(\omega)}{\sqrt{1/3\ell(\ell+1)}}$$

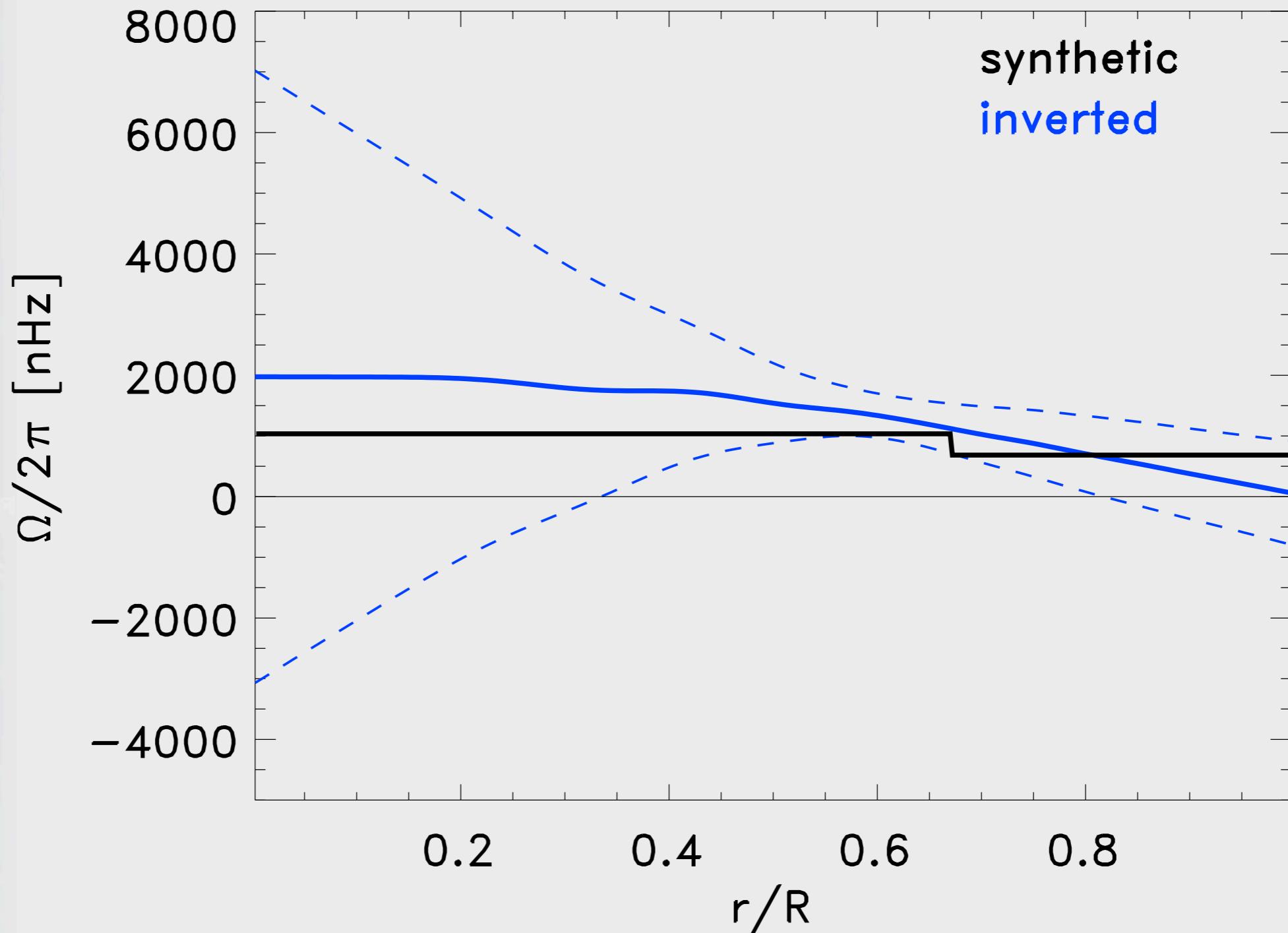


Radial Differential Rotation of Sun-like Star

- Stellar model of Sun-like star (kernels)
- Synthetic rotation profile
- Rotational splittings
+ uncertainties on the splittings
- Inversion



Radial Differential Rotation of Sun-like Star

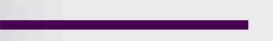
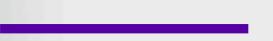
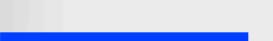
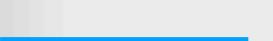
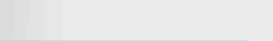
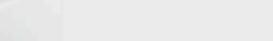
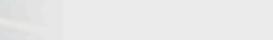
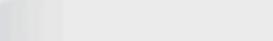


Ensemble Inversions

- PLATO will be launched in 2024
PLAnetary Transits and Oscillations of stars
- Observe many more stars than *Kepler*
- Two long duration observations ~3 years long
- Assume that rotation is similar

Ensemble Inversions

- Fifteen main sequence stellar models ranging from F to K type

	$M/M_{\odot}=0.8$	$\text{Fe}/\text{H}= 0.5$	$\text{BCZ}=0.653R_*$	$\text{Teff}=4566 \text{ K}$
	$M/M_{\odot}=0.8$	$\text{Fe}/\text{H}= 0.5$	$\text{BCZ}=0.639R_*$	$\text{Teff}=4700 \text{ K}$
	$M/M_{\odot}=0.8$	$\text{Fe}/\text{H}= 0.5$	$\text{BCZ}=0.615R_*$	$\text{Teff}=4878 \text{ K}$
	$M/M_{\odot}=0.8$	$\text{Fe}/\text{H}=-0.5$	$\text{BCZ}=0.726R_*$	$\text{Teff}=5619 \text{ K}$
	$M/M_{\odot}=1.1$	$\text{Fe}/\text{H}= 0.5$	$\text{BCZ}=0.672R_*$	$\text{Teff}=5640 \text{ K}$
	$M/M_{\odot}=1.1$	$\text{Fe}/\text{H}= 0.5$	$\text{BCZ}=0.709R_*$	$\text{Teff}=5657 \text{ K}$
	$M/M_{\odot}=1.1$	$\text{Fe}/\text{H}= 0.5$	$\text{BCZ}=0.704R_*$	$\text{Teff}=5721 \text{ K}$
	$M/M_{\odot}=0.8$	$\text{Fe}/\text{H}=-0.5$	$\text{BCZ}=0.719R_*$	$\text{Teff}=5763 \text{ K}$
	$M/M_{\odot}=0.8$	$\text{Fe}/\text{H}=-0.5$	$\text{BCZ}=0.706R_*$	$\text{Teff}=5908 \text{ K}$
	$M/M_{\odot}=1.4$	$\text{Fe}/\text{H}= 0.5$	$\text{BCZ}=0.747R_*$	$\text{Teff}=5991 \text{ K}$
	$M/M_{\odot}=1.4$	$\text{Fe}/\text{H}= 0.5$	$\text{BCZ}=0.808R_*$	$\text{Teff}=6267 \text{ K}$
	$M/M_{\odot}=1.4$	$\text{Fe}/\text{H}= 0.5$	$\text{BCZ}=0.838R_*$	$\text{Teff}=6433 \text{ K}$
	$M/M_{\odot}=1.1$	$\text{Fe}/\text{H}=-0.5$	$\text{BCZ}=0.905R_*$	$\text{Teff}=6686 \text{ K}$
	$M/M_{\odot}=1.1$	$\text{Fe}/\text{H}=-0.5$	$\text{BCZ}=0.880R_*$	$\text{Teff}=6703 \text{ K}$
	$M/M_{\odot}=1.1$	$\text{Fe}/\text{H}=-0.5$	$\text{BCZ}=0.895R_*$	$\text{Teff}=6713 \text{ K}$

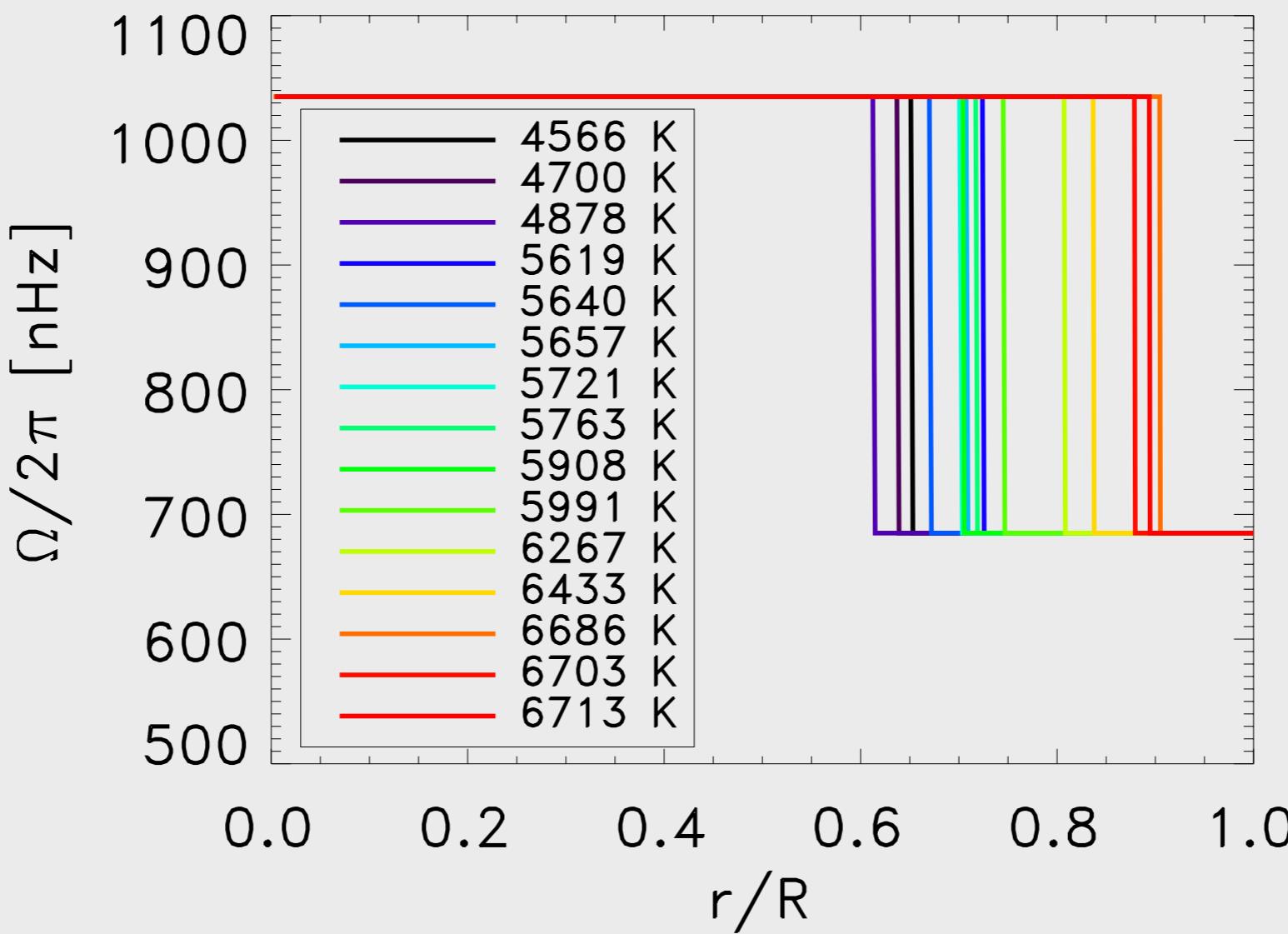
K

G

F

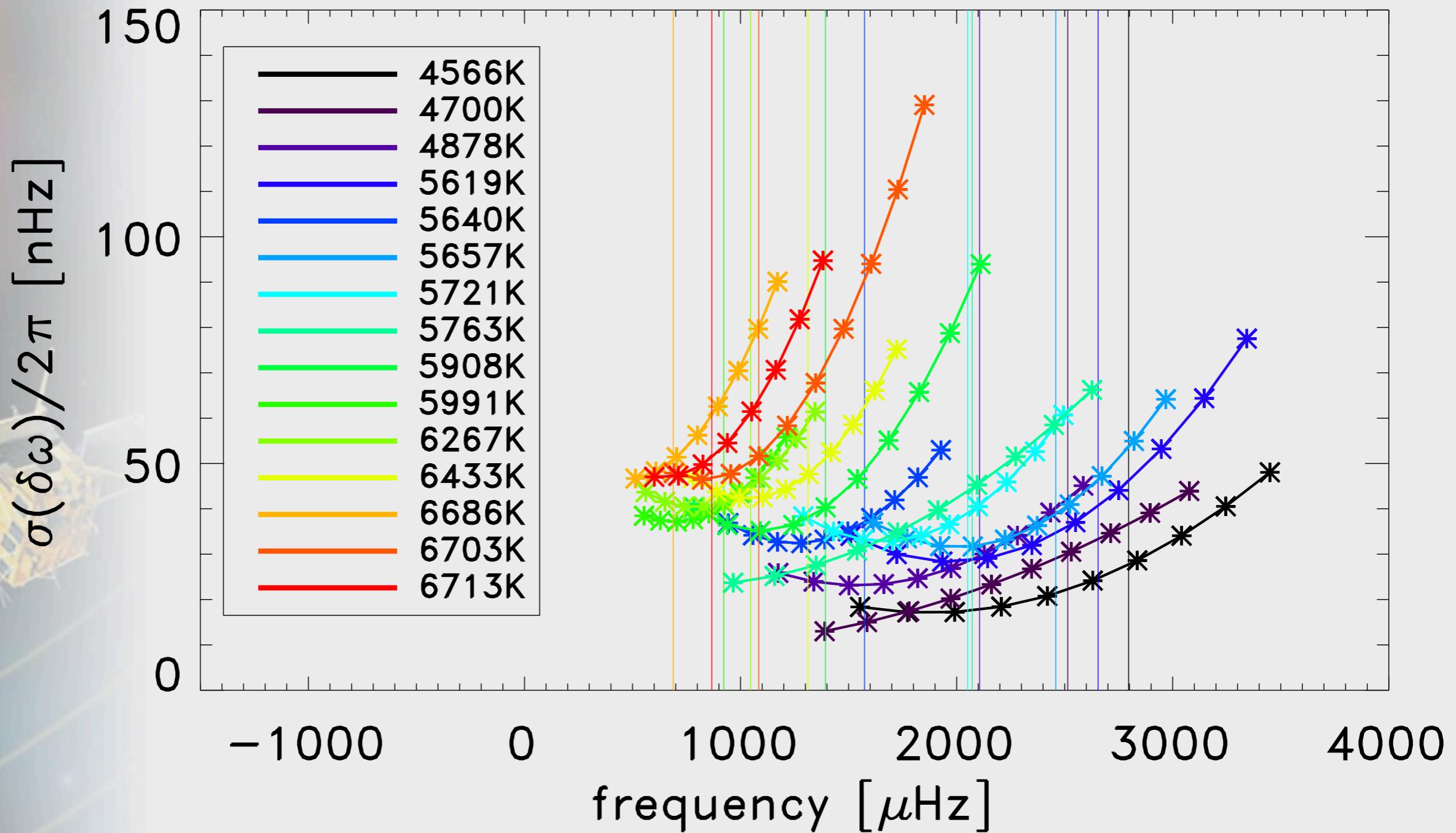
Ensemble Inversions

- Synthetic rotation rates
 - identical rotation rates
 - discontinuity at the BCZ--> rotational splittings



Ensemble Inversions

- Uncertainties for 3 year long observations



Ensemble Inversions

all observed splittings

$$\delta\omega_i = \int_0^R K_i(r)\Omega(r)dr + \sigma(\delta\omega_i)$$

average rotation

all uncertainties

all the stellar models

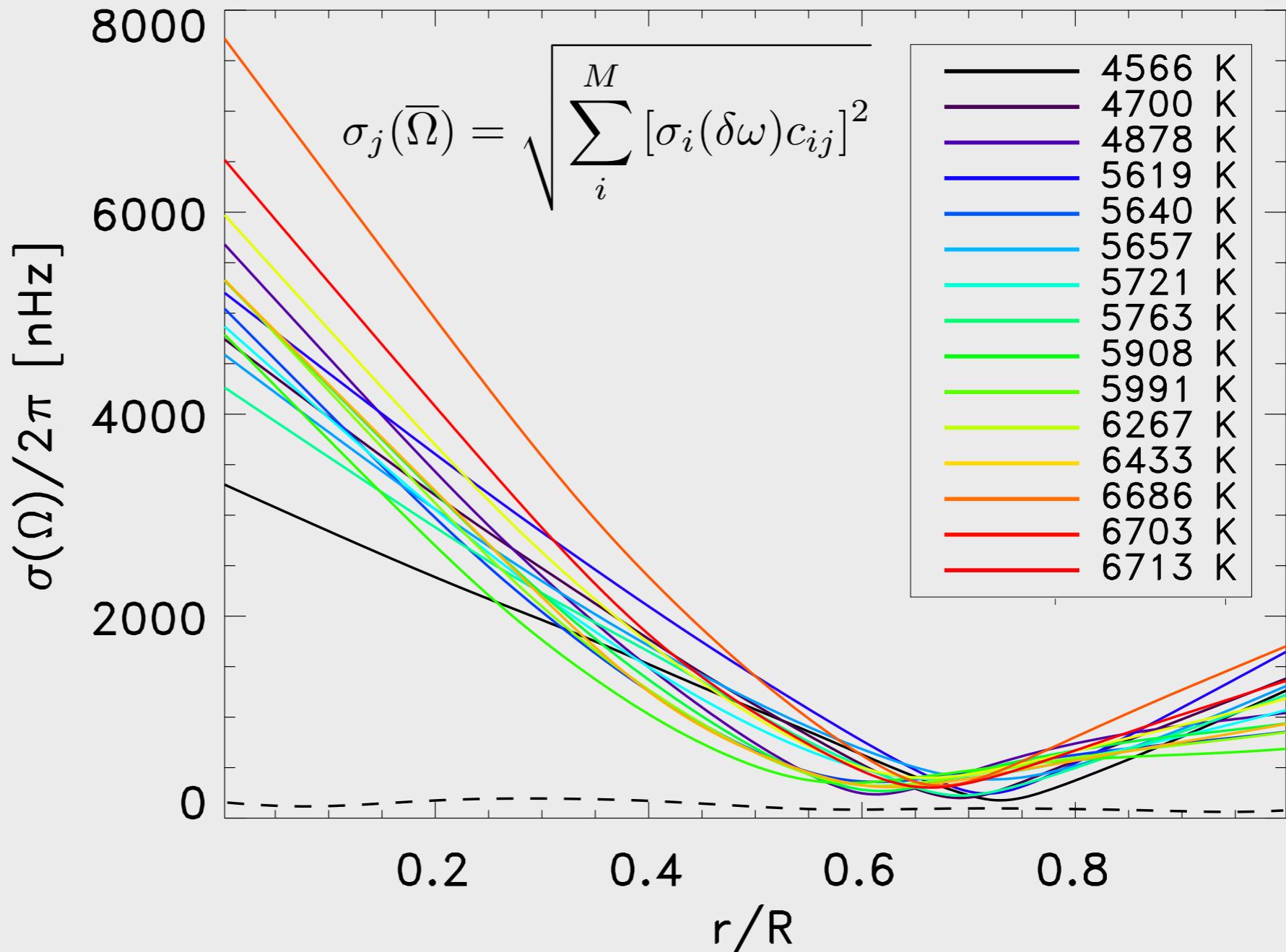
RLS Inversion

$$\sum_{i=1}^M \left[\delta\omega_i - \int_0^R \mathcal{K}_i(r)\bar{\Omega}(r)dr \right]^2 + \text{smoothing}$$

Ensemble Inversions

- Fifteen stellar models ranging from F to K type
- Synthetic rotation rates
 - identical rotation rates
 - discontinuity at the BCZ
- Rotational splittings
- Uncertainties for 3 year long observations
- Inversion for the average rotation profile
 - do the uncertainties decrease?

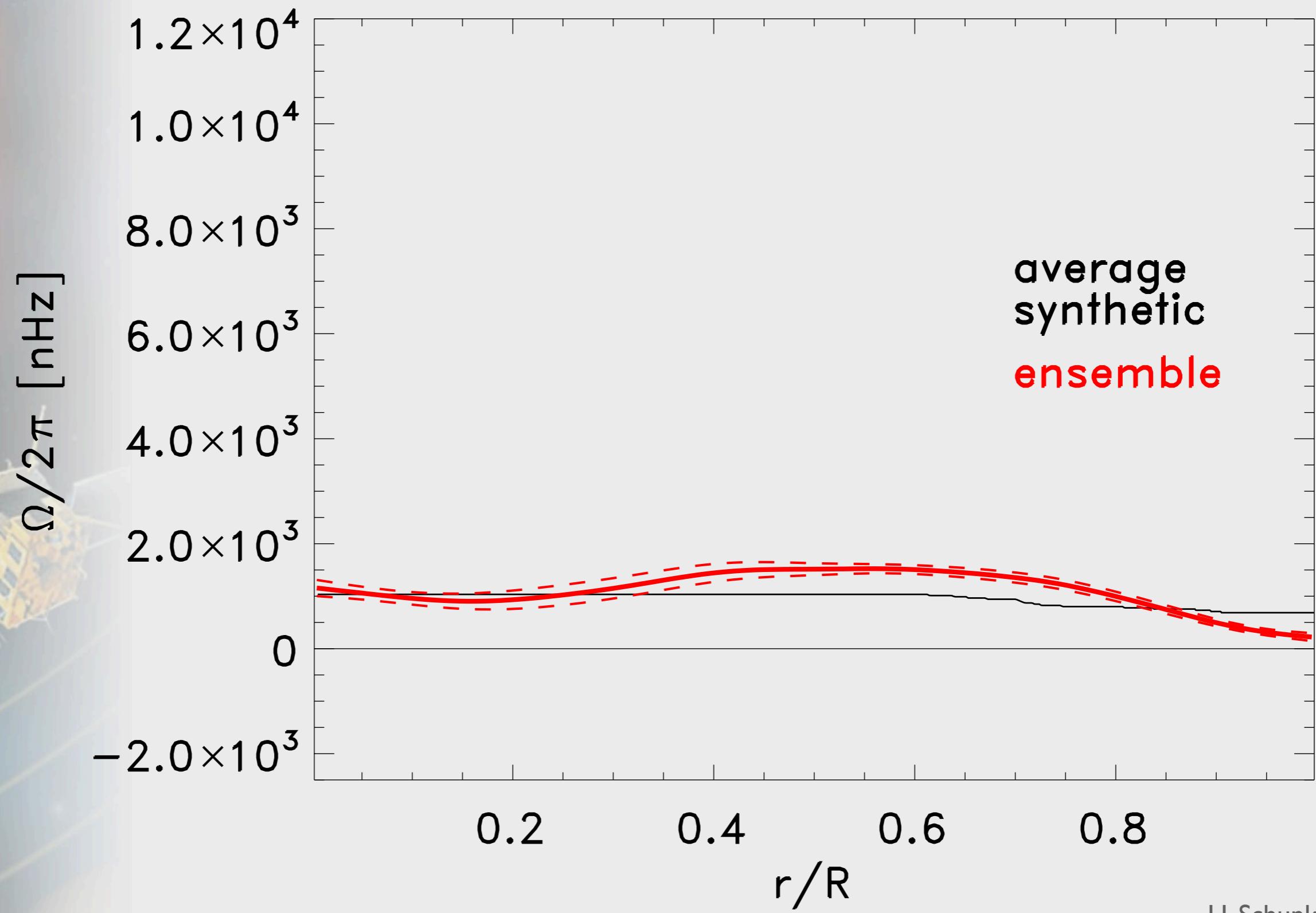
Ensemble Inversions



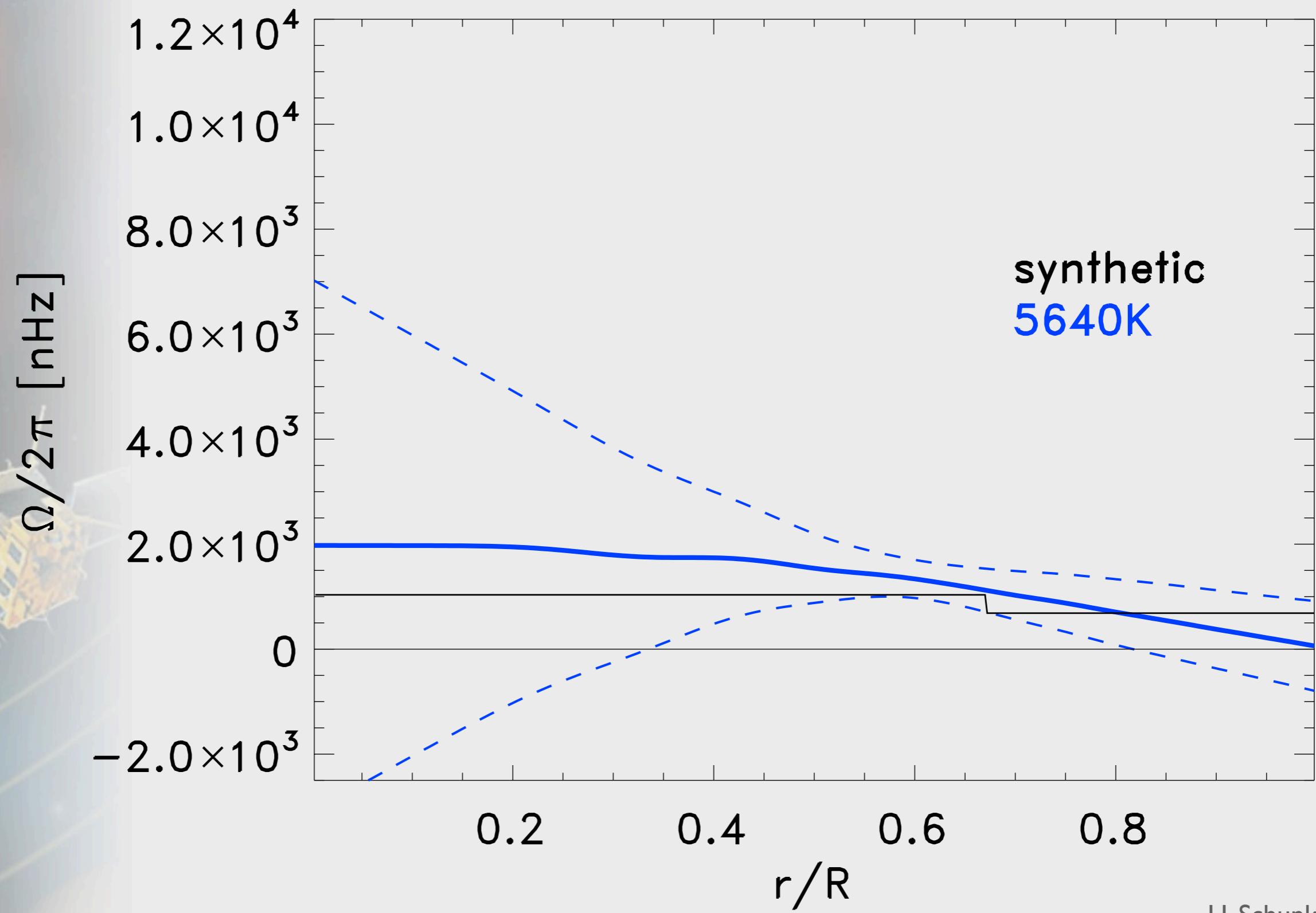
Uncertainties

- similar for all stars regardless of type
- decrease with \sqrt{N}

Ensemble Inversions

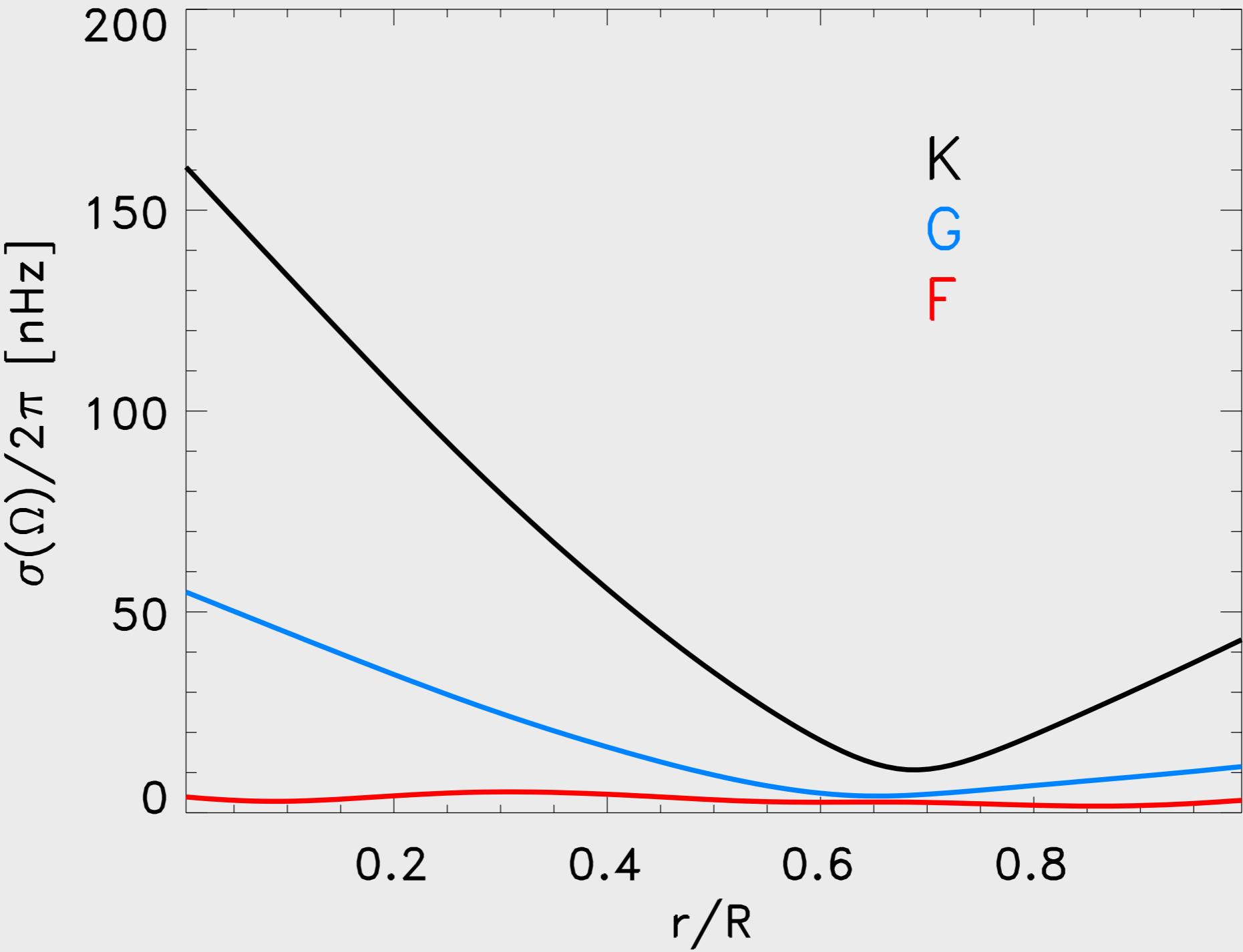


Ensemble Inversions

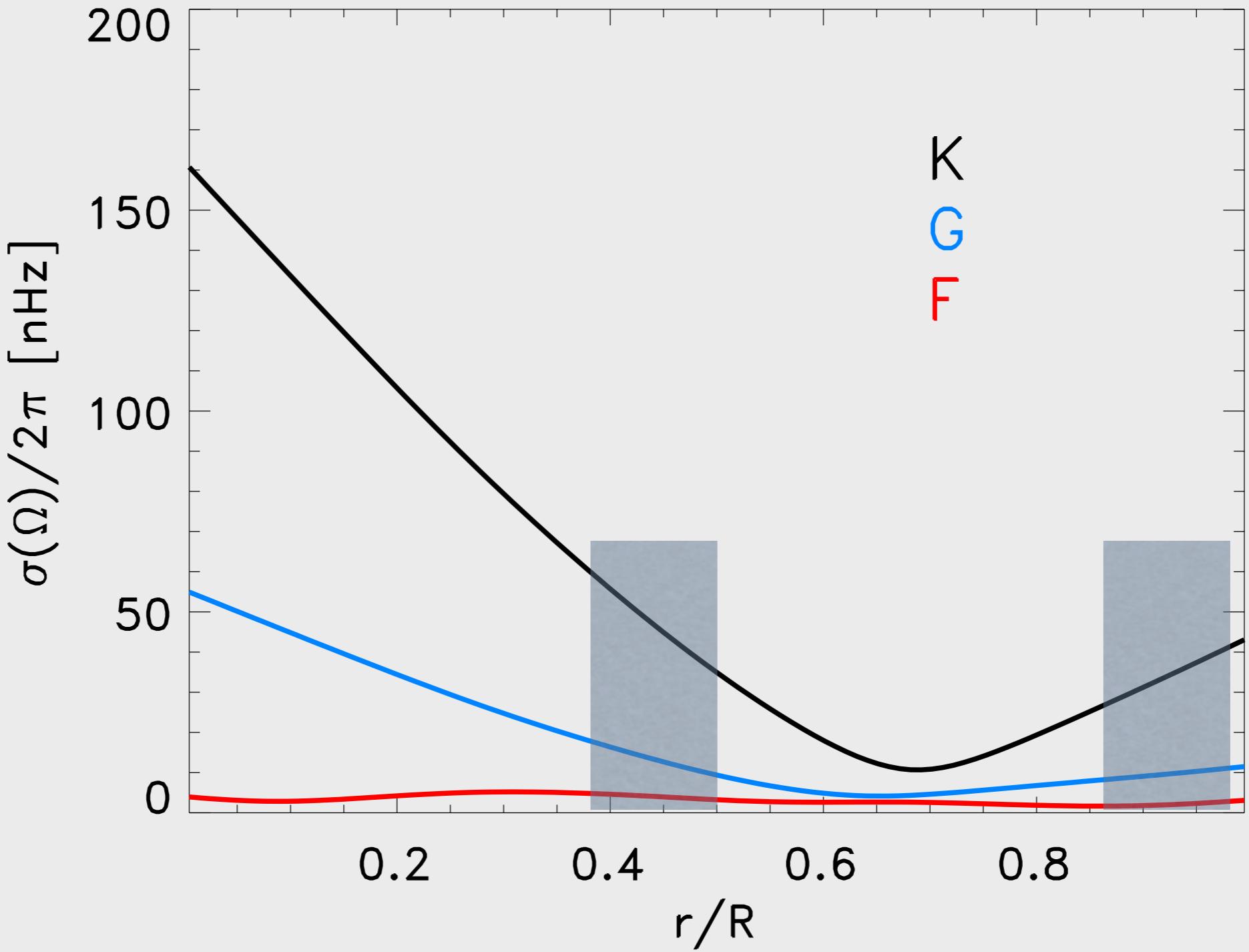


- Long Observation Fields: 2-3 years
2,700 stars F5 to K7 type
 $mv < 8$
50 sec cadence
34 ppm/h
- 65% (1800) F dwarfs,
30% (800) G dwarfs,
5% (100) K dwarfs
 $\log g > 3.5$ and $T_{eff} < 6510$ K

Rotation vs Stellar Type



Rotation vs Stellar Type



Detect a minimum rotational difference of ~ 100 nHz

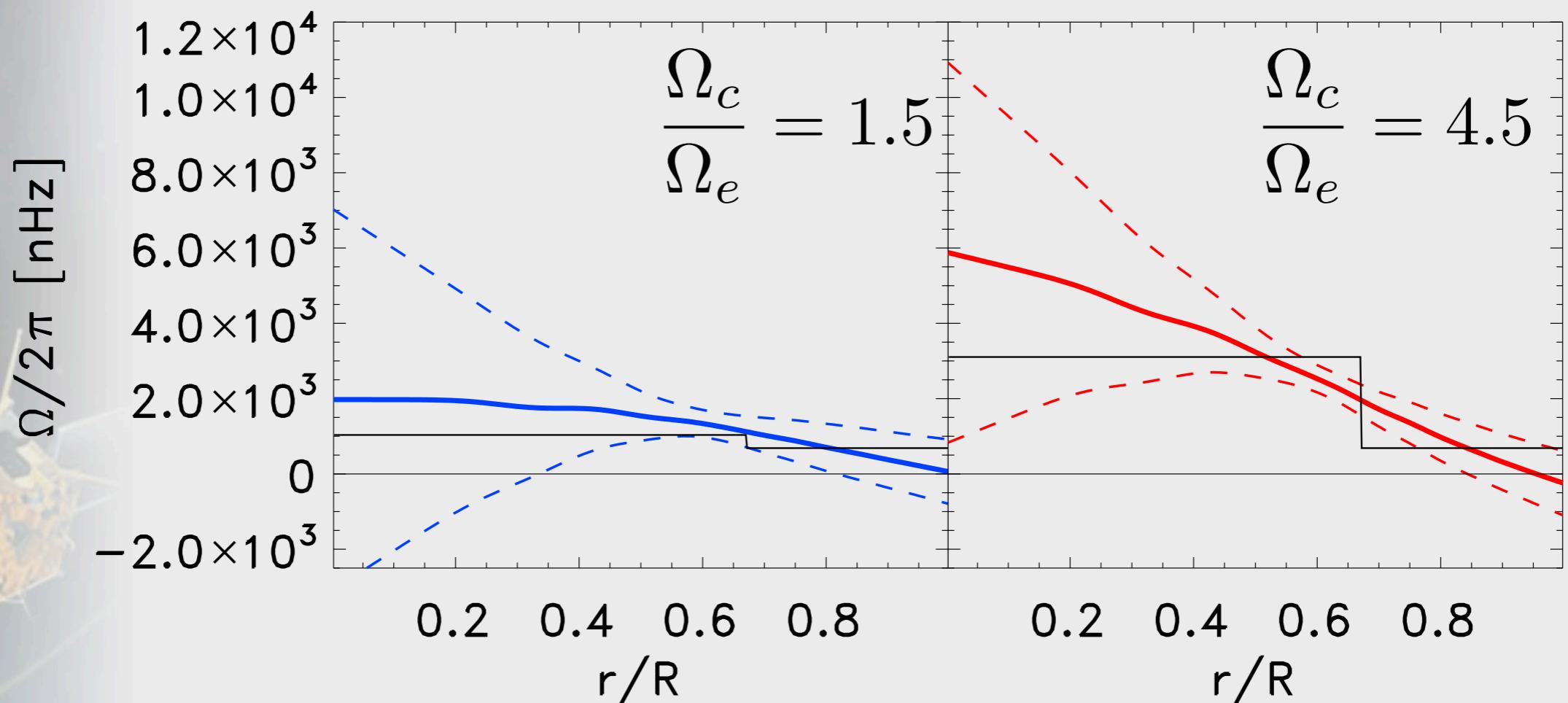
Outlook

- PLATO will observe 1000s of bright Sun-like stars
- Ensemble inversions: reduced uncertainties
- Differentiate between rotation of F, G, K type of stars
- Different inversion method?
- Comparison between starspot and seismic rotation periods may reveal more about
 - the depth sensitivity of starspots
 - latitudinal differential rotation

Radial Differential Rotation of Sun-like Star

- Increase the core rotation rate x3 $\Omega_c \approx 6\Omega_\odot$

$$P_c \approx 4 \text{ days}$$



- Detect a rotational difference of ~ 2000 nHz